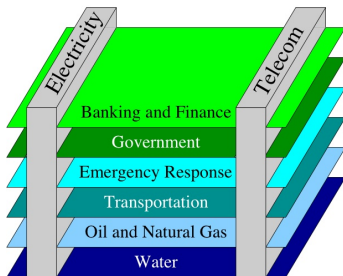
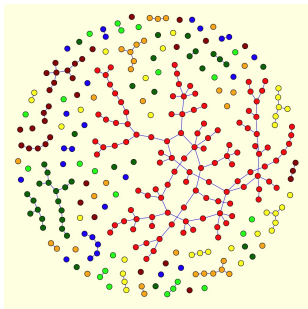


# Predicting and controlling systems of interdependent networks: Exploiting interdependence for control



FY2013 Multidisciplinary University Research Initiative (MURI)  
Topic: Controlling Collective Phenomena in Complex Networks

U. S. Army Research Laboratory and the U. S. Army Research  
Office contract/grant number W911NF-13-1-0340

# The core team

- Raissa M. D'Souza, UC Davis
- Jim Crutchfield, UC Davis
- Leonardo Duenas-Osorio, Rice University
- Jessica Flack, University of Wisconsin
- David C. Krakauer, University of Wisconsin
- Mehran Mesbahi, University of Washington
- Michael Roukes, California Institute of Technology

A diverse team, spanning an array of fields: Network Science, Information Theory, Control Theory, Critical Infrastructure, Sensitivity Analysis, Statistics, Nonlinear Dynamics, Animal Behavior, Nanoscale device physics...

## **State-dependent, dynamic networks**

Dynamics of networks coupled to dynamics on networks, especially in noisy, dynamic environments

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- Task 1. Collective Computation
- Task 2. Interdependent and layered networks
- Task 3. Exploiting interdependence for control

# Task 1. “Collective Computation”

- **Task 1.1: Network Information Theory and Functional Pattern Formation:**  
Crutchfield (Lead), Flack & Krakauer, Roukes (pattern formation)
- **Task 1.2: Collective Computation (Game theoretic underpinnings: Network function and structure):**  
Flack (Lead), Krakauer, Crutchfield, Roukes (node knock-out experiments; subsystems with competing objectives)
- **Task 1.3: Control of state-dependent dynamic networks:**  
Mesbahi (Lead), Flack, Crutchfield, D’Souza, Roukes (state-dependence)

## Task 2. Interdependent and layered networks

- **Task 2.1: Structure of interdependent networks:**  
D'Souza (Lead) & Dueñas-Osorio
- **Task 2.2: Function of interdependent networks:**  
D'Souza & Dueñas-Osorio (co-leads), Roukes  
(synchronization)
- **Task 2.3: Beyond the adjacency matrix: New mathematical representations for networks of networks:**  
Mesbahi (Lead), D'Souza, Dueñas-Osorio
  - Cartesian products
  - Kroneker graphs
  - hypergraphs

## Task 3. Exploiting interdependence for control

- **Task 3.1: Multi-modal recovery and distributed control:**  
Dueñas-Osorio (Lead), D'Souza, Mesbahi
- **Task 3.2: Control theory formulations:**  
Mesbahi (Lead), Dueñas-Osorio, D'Souza, Roukes (layered arrays?)

# Fundamental objectives stated in proposal

- To understand the mechanisms for the emergence of structure and function and for controlling them.
- To identify feedback, co-evolution and opportunities for control.
- To assess fundamental bounds on effective means of influencing dynamic networks through control- and system-theoretic formalisms.
- To create new mathematical models of interdependent networks.
- To uncover coupling and recovery processes from empirical databases.
- To reveal feasible control strategies for critical infrastructure, coupled systems, and social response.
- To reveal the mechanisms for emergence of synchronization and global clocks in noisy dynamic environments.
- To quantify the effects of node knock-out and compensatory perturbations for multi-system control.
- To build a vibrant community of researchers actively working on control of collective phenomena in complex multi-networks.
- To provide transdisciplinary training to the next generation of scientists and engineers.

# Anticipated Outcomes

- Network interventions that prevent cascades of failure in critical infrastructures
- Novel control schemes relying on control actions and local interventions
- Rigorous principles for multi-modal recovery of heterogeneous systems
- Designing incentives that align human behavior with the capabilities of technological networks
- Design of networks of nonlinear NEMs oscillators that exploit coupling and nonlinearity to create coherent motion
- New mathematical structures for representing and analyzing networks-of-networks, especially with respect to control theory
- Fundamental bounds on controllability of interdependent networks and rigorous techniques to identify which network layers are easiest to steer.



# Summary of deliverables (details on pg 19-20)

Schedule of Major Project Activities	
Year 1	<ul style="list-style-type: none"><li>– Proposal for semester program in Year 3 sent to IPAM board for approval* (In progress)</li><li>– Team meeting at UCD; intro to KeckCAVES (Nov 12, and today)</li><li>– Mini-conference on control of interdependent networks at UC Davis (Leverages NSF funded “Shocks cascading through coupled networks” conference) (NetSci 2014: Tutorials &amp; Satellite meeting)</li><li>– First postdoc and student rotations (continue throughout project)</li><li>– First student and faculty visits to ARL (cont throughout project)</li></ul>
Year 2	<ul style="list-style-type: none"><li>– Students attend SFI Summer School (1-2 students now and in each subsequent year)</li><li>– Team meeting at Santa Fe Institute (or partner inst)</li><li>– Sessions on control of interdependent networks organized at intl. conferences</li><li>– New graduate courses developed in support of this MURI (materials released online)</li></ul>

\*(Simmons Inst might also work as well as IPAM)

# Summary of deliverables (details on pg 19-20)

	<b>Schedule of Major Project Activities, cont.</b>
Year 3	<ul style="list-style-type: none"><li>– Semester program at IPAM</li><li>– Team meeting at Caltech, University of Wisconsin or SFI</li><li>– Special volume of <i>J. Complex Networks</i> on control of interdependent networks</li><li>– First batch of postdocs move onto positions in Academia, Industry or National Labs</li></ul>
Year 4	<ul style="list-style-type: none"><li>– Team meeting and mini-conference at UC Davis showcasing Keck-CAVES tools</li><li>– Sessions on control of interdependent networks organized at intl. conferences</li><li>– First PhD students trained under this MURI graduate</li></ul>
Year 5	<ul style="list-style-type: none"><li>– Team meeting (at Wisc, SFI, Rice or Wash.)</li><li>– Postdocs move onto positions in Academia, Industry or National Labs</li><li>– Final PhD students trained under this MURI graduate</li><li>– Culminating international conference at Santa Fe Institute</li></ul>

## Some accomplishments to date

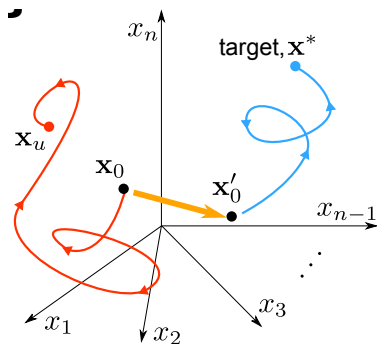
- Team-wide, in-person meeting at UCD on Nov 12th.
  - Cross-cutting threads articulated (e.g., synchronization; spectral statistics; systems of multiple components with only partially aligned interests)
  - Concrete research projects (e.g., Cartesian products for critical infrastructure; NEMs systems to model collective computation; spillover in layered networks)
- Airlie Chapman joins team as postdoctoral scholar and rotation to UCD.
- Flack, D'Souza and Spencer (Google, letter of support for MURI) co-editors of a special volume of *IEEE Spectrum*.
- Crutchfield visit to UWisconsin, Nov 2013.
- NetSci 2014 events organized: Tutorials (Airlie Chapman); Satellite meeting on control of networks (Mesbahi, D'Souza)

# Goals for today

- Make more crisp the concrete research projects and collaboration plans
- Guidance from Sam Stanton — vision for success
- Deeper understanding of the experimental systems and real-world data sets
  - NEMs Oscillators – today and planning 2-3 years out
  - Macaque monkey societies
  - Critical infrastructure

# Controlling networks

A network with  $n$  nodes  
an  $n$ -dimensional phase space:



S.P. Cornelius, W.L. Kath, and A.E. Motter, arXiv:1105.3726 (2011),  
Nature Communications (2013).

- **Strong Control:** want to control the state of each node.
- **Weak/Partial Control:** want to steer the system.
- **Controlling self-organizing systems especially challenging:** the system responds to the controller.
- **State dependence:** of system, including the environment