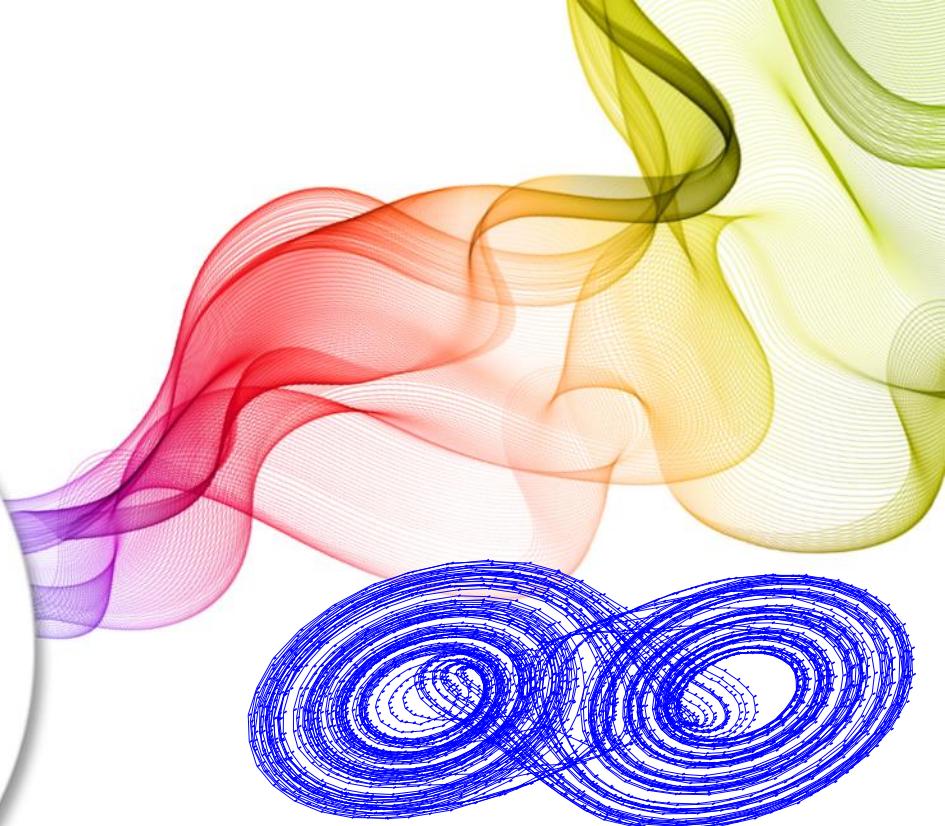


Dany  
Masante

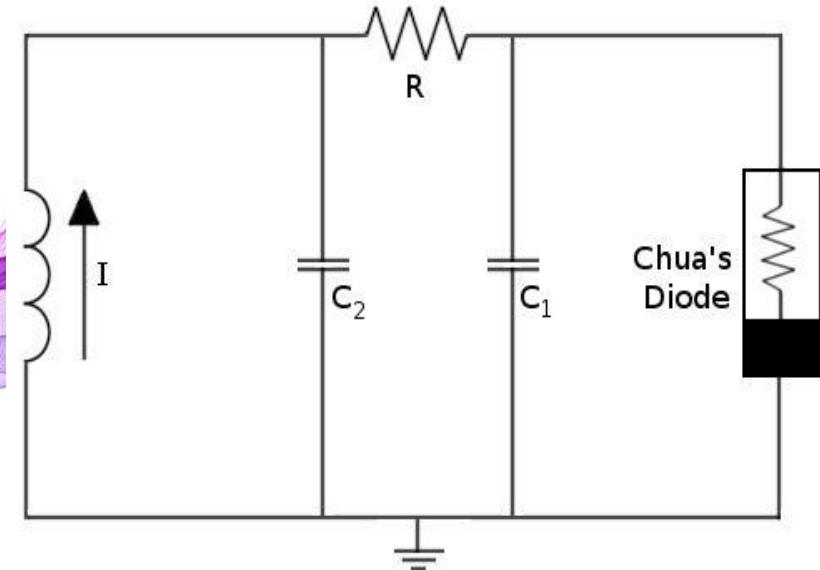
# Chua Circuit Experimental Realization



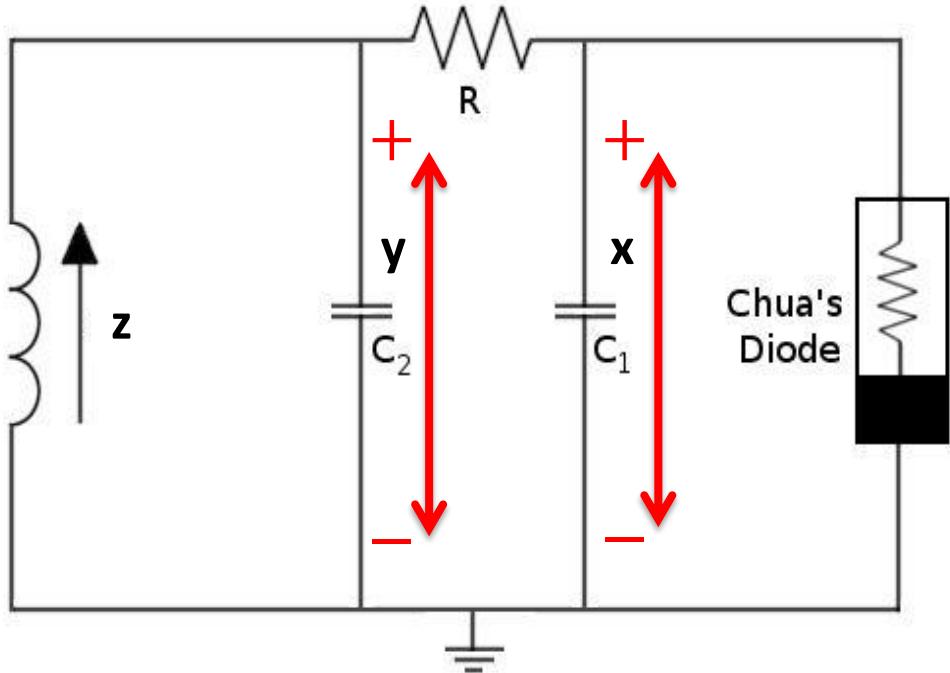
**PHY256: NCASO – Final Project**  
**UC Davis Physics**  
**6 June 2017**

1

# Chua's Circuit



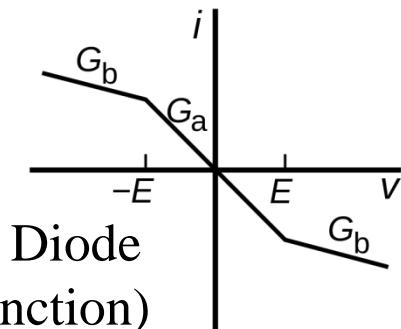
# The equations of motion



$$\dot{x}'' \rightarrow \frac{dV_1}{dt} = \left[ \frac{1}{RC_1} \right] ((V_2 - V_1) - R * g(v_1))$$

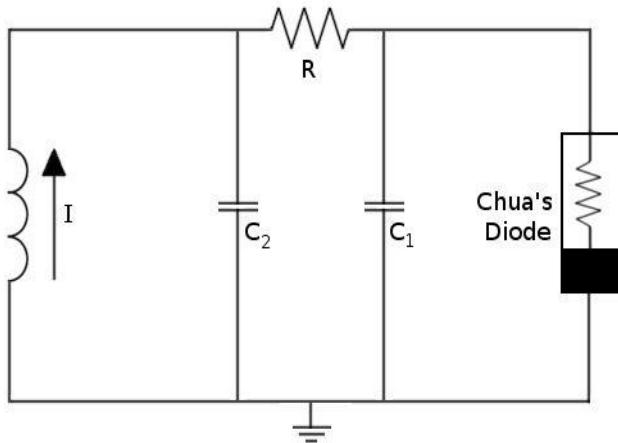
$$\dot{y}'' \rightarrow \frac{dV_2}{dt} = \left[ \frac{1}{RC_2} \right] ((V_1 - V_2) - R * i_L)$$

$$\dot{z}'' \rightarrow \frac{di_L}{dt} = \left[ \frac{1}{L} \right] (-v_2)$$

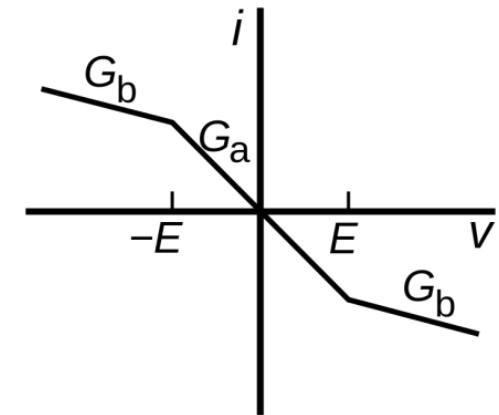


Where  $g(x)$  is Chua's Diode  
(piecewise function)

# Three Fixed Points



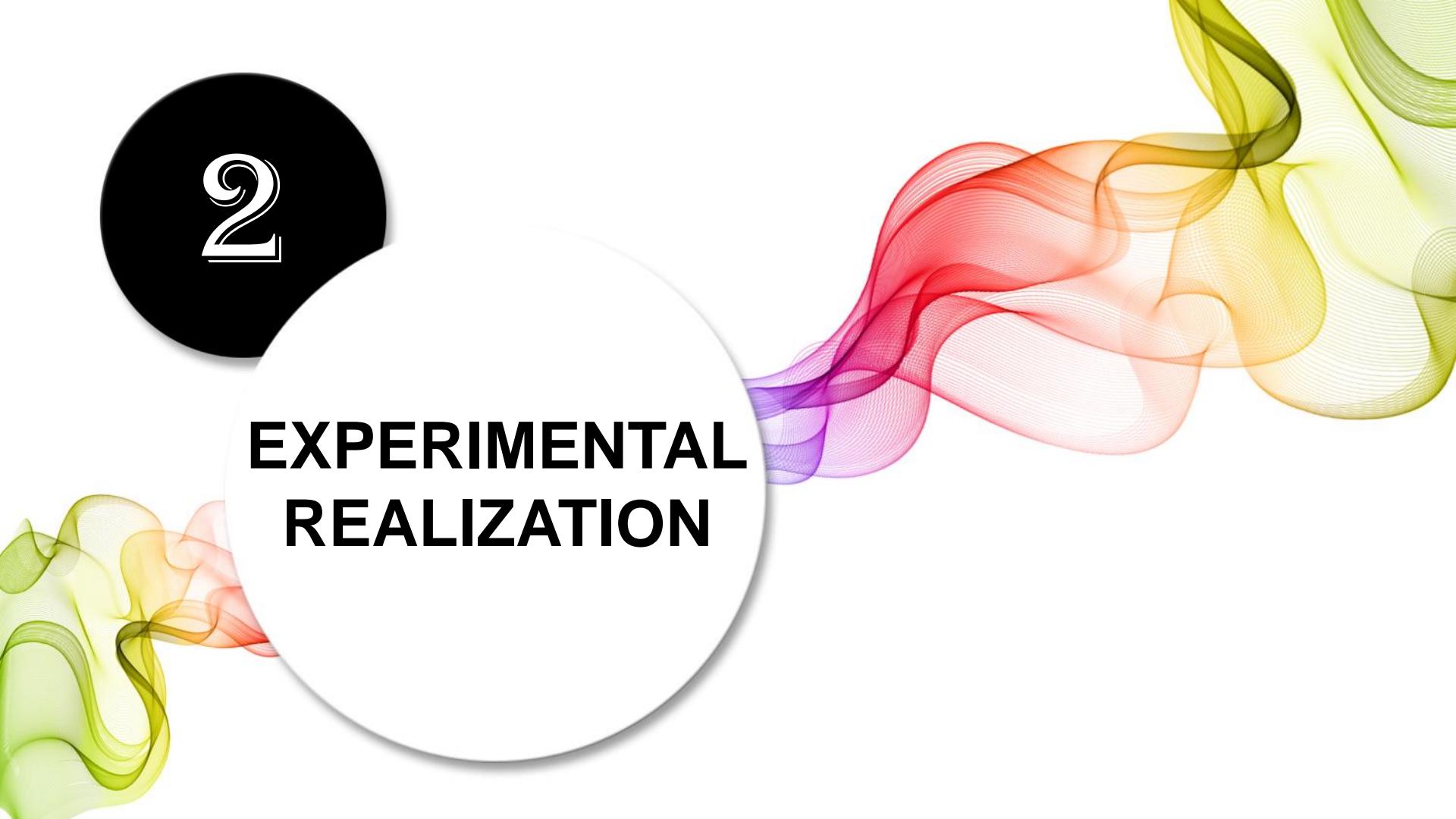
$$p_0 = [0, \quad 0, \quad 0]$$



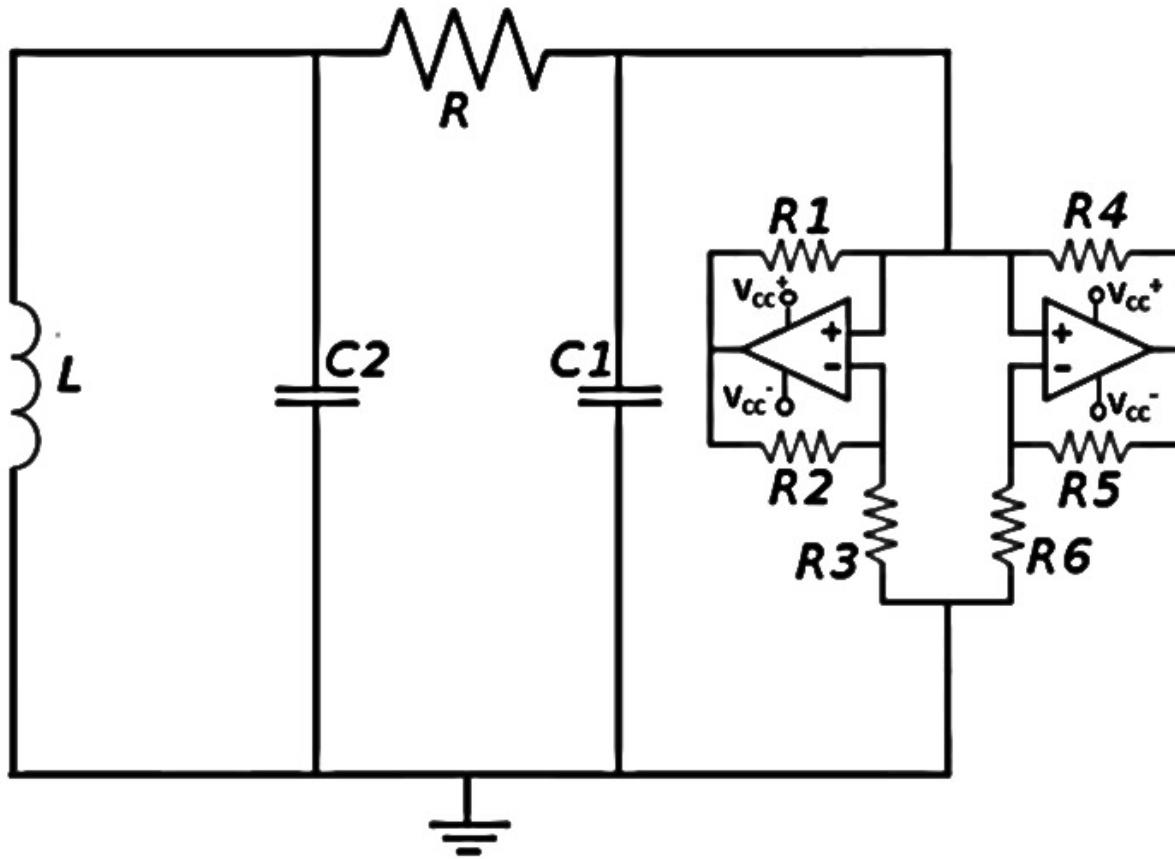
$$p_{1,2} = \pm \left[ \frac{-E(G_b - G_a)(r_L + R)}{1 + (R + r_L)G_b}, \quad \frac{-E(G_b - G_a)(r_L)}{1 + (R + r_L)G_b}, \quad \frac{+E(G_b - G_a)(r_L)}{1 + (R + r_L)G_b} \right]$$

2

## EXPERIMENTAL REALIZATION



# Experimental Realization



Where

$$R_1 = 220 \text{ } [\Omega]$$

$$R_2 = 220 \text{ } [\Omega]$$

$$R_3 = 2.2 \text{ } [k\Omega]$$

$$R_4 = 22 \text{ } [k\Omega]$$

$$R_5 = 22 \text{ } [k\Omega]$$

$$R_6 = 3.3 \text{ } [k\Omega]$$

$$C_1 = 10 \text{ } [nF]$$

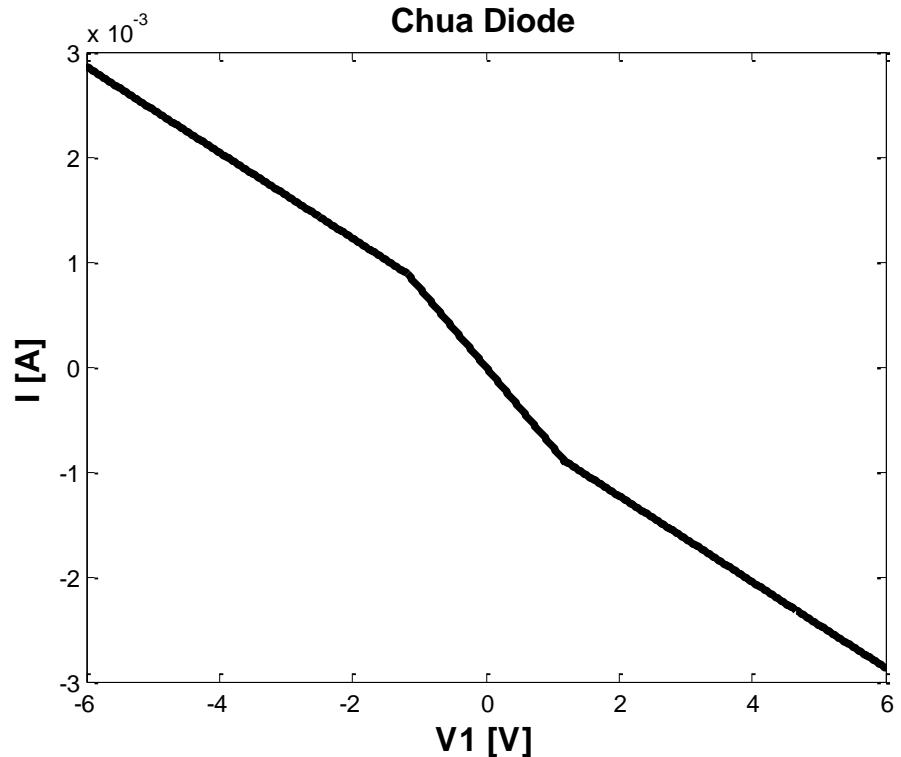
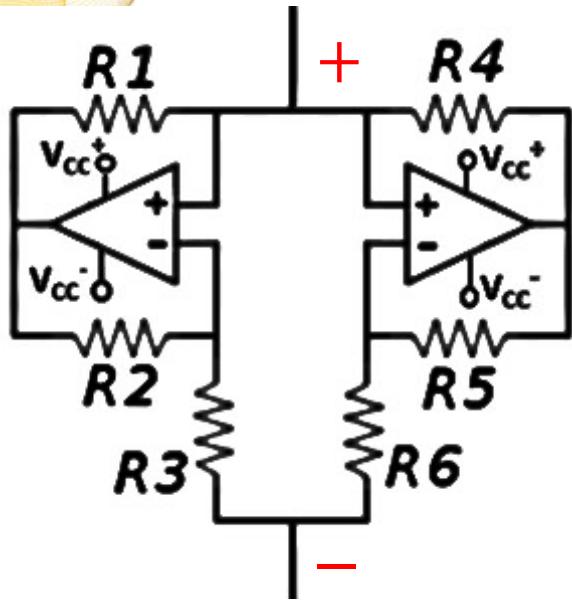
$$C_2 = 100 \text{ } [nF]$$

$$L = 18 \text{ } [mH]$$

And  $R$  is a potentiometer  
(variable resistor)

# Chua Diode

$$g(v_1) = \begin{cases} m_0 v_1 + (m_0 - m_1)E_1, & v_1 \leq E_1 \\ m_1 v_1, & -E_1 \leq v_1 \leq E_1 \\ m_0 v_1 + (m_1 - m_0)E_1, & v_1 \geq E_1 \end{cases}$$



Where

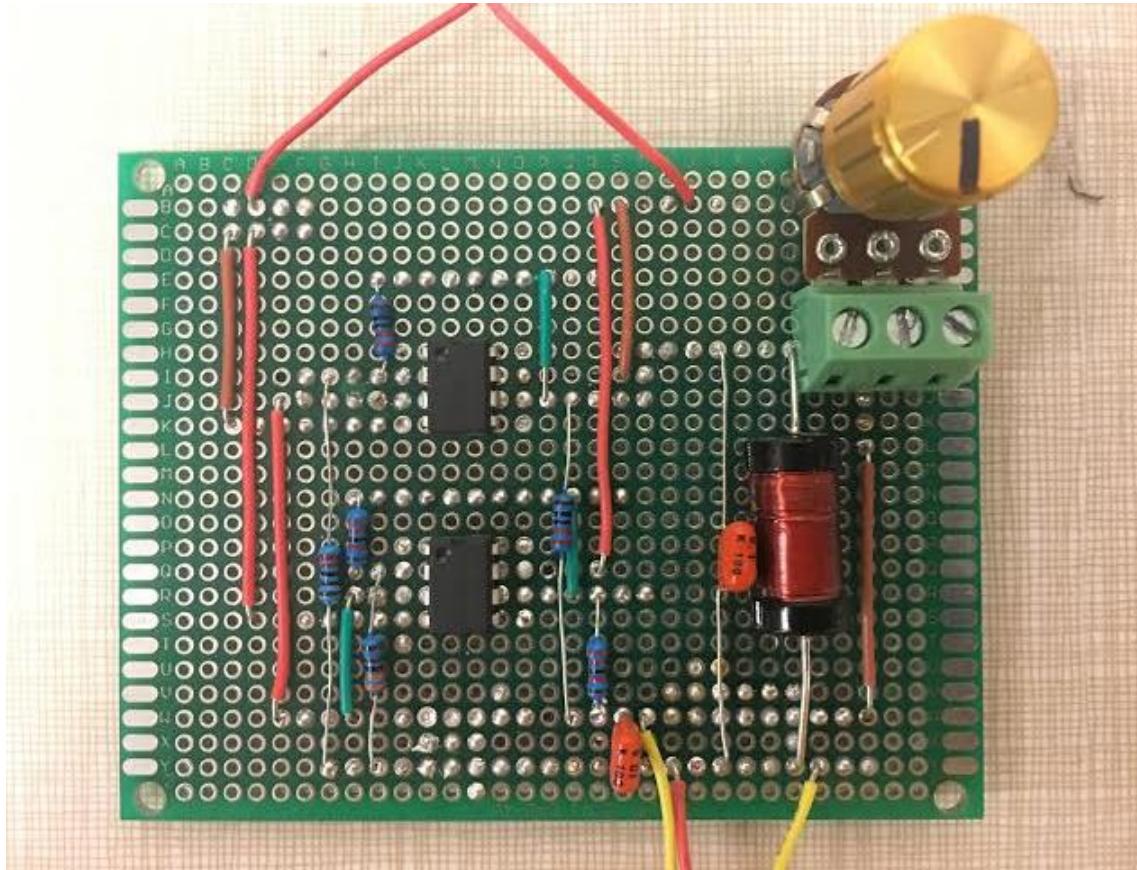
$$m_0 = \frac{1}{R_4} - \frac{1}{R_3}, \quad m_1 = -\frac{1}{R_3} - \frac{1}{R_6}, \quad E_1 = \frac{R_3}{(R_2+R_3)} E_{sat}$$

# List of Materials

Device	Stock Code	Quantity	Description
Capacitor	Mapln Sc Series	2	Metallized Polyester Film (MKT) Capacitors
Inductor	PCH45X186KLT	1	Axial Lead Power Choke
Resistor	TOPCOFRLD008	6	Metal Film full range resistor
Potentiometer	B01LYHMKNN	1	Logarithmic Dual Rotary Potentiometer
Operational Amplifier	TI6PCSUA741CP	2	General Purpose Operational Amplifier

All elements are Rohs complilant

# Experimental Realization



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# NUMERICAL

# Numerical Realization

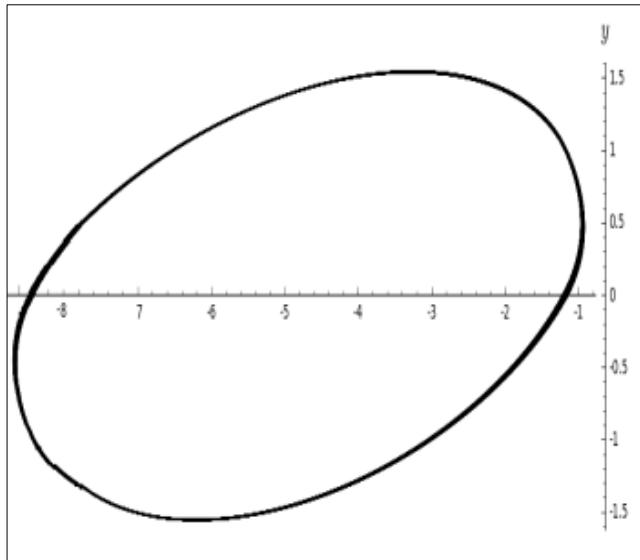
- Sagemath
- Dimensionless Chua Eqs.
- Finite difference method
- Timestep = 0.000001
- Iterations = 100000
- Discarded (transients)= 10%
- Initial Conditions= Aleatory negative initial conditions ( -10 to 0 )



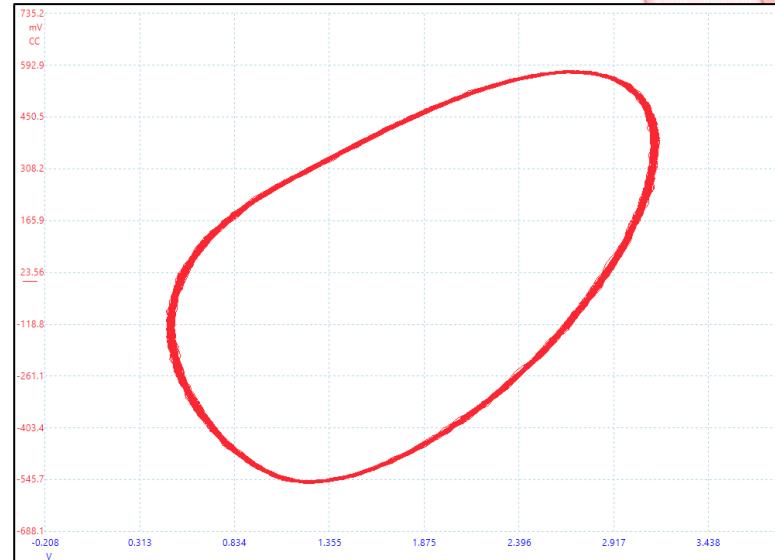
# RESULTS



# Numerical VS Experimental



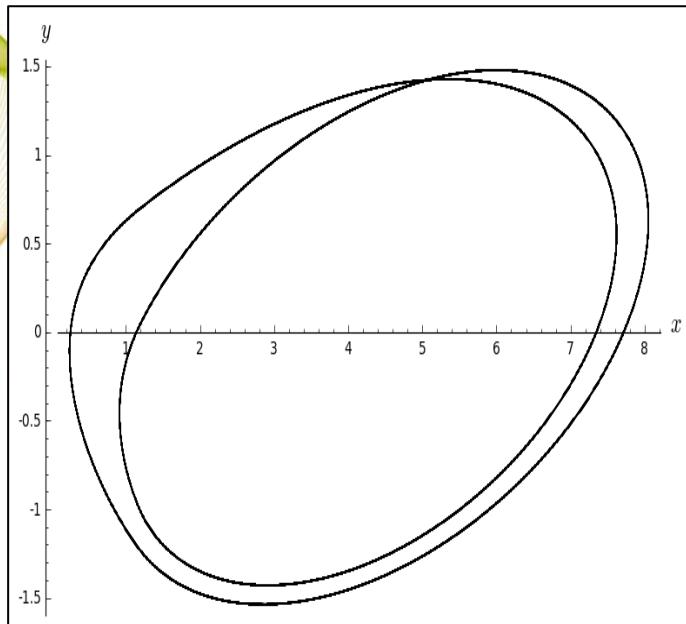
$R = 2015 \text{ } [\Omega]$



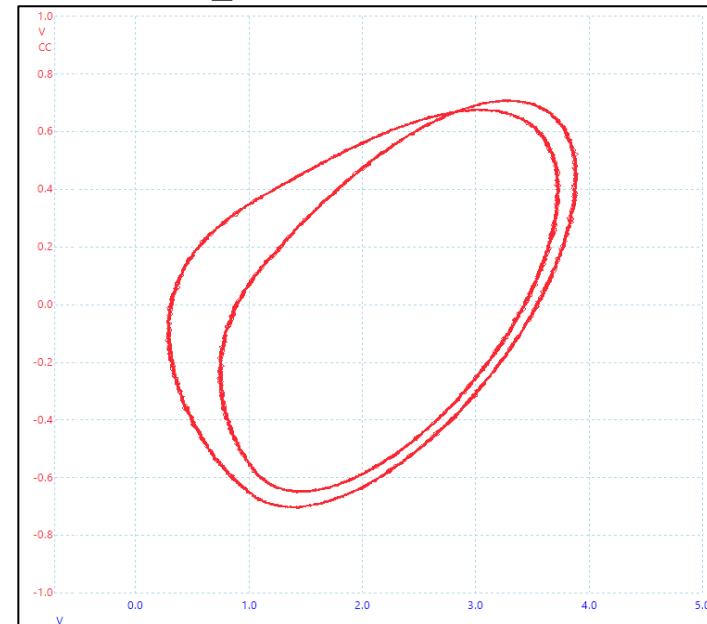
$R = 1777 \text{ } [\Omega]$

$\Delta = 11.81\%$

# Numerical VS Experimental



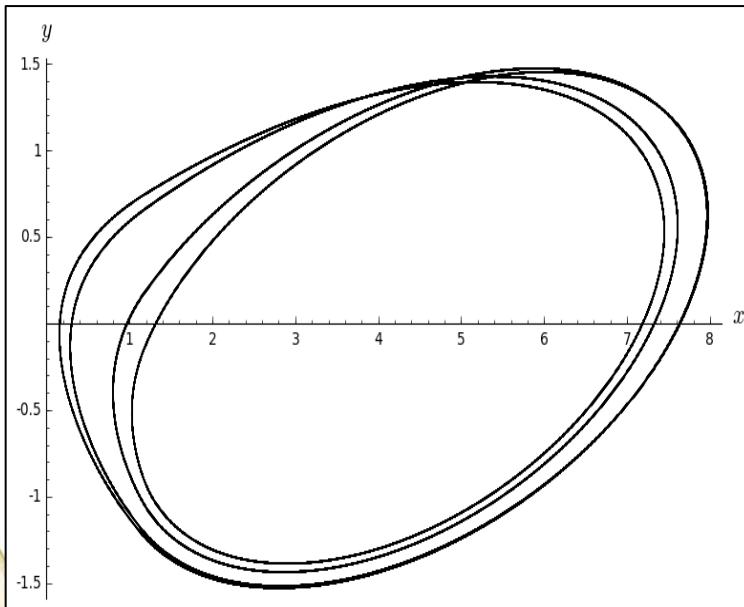
$R = 2001 [\Omega]$



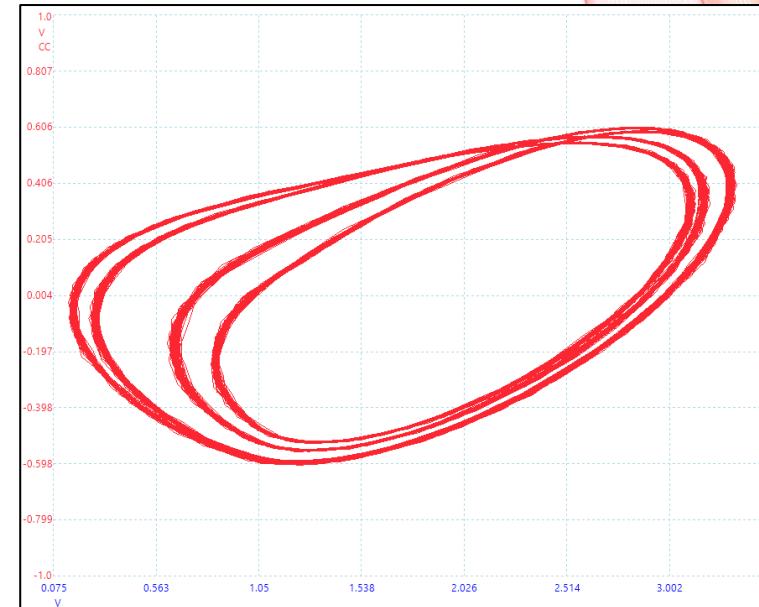
$R = 1714 [\Omega]$

$\Delta = 14.34\%$

# Numerical VS Experimental



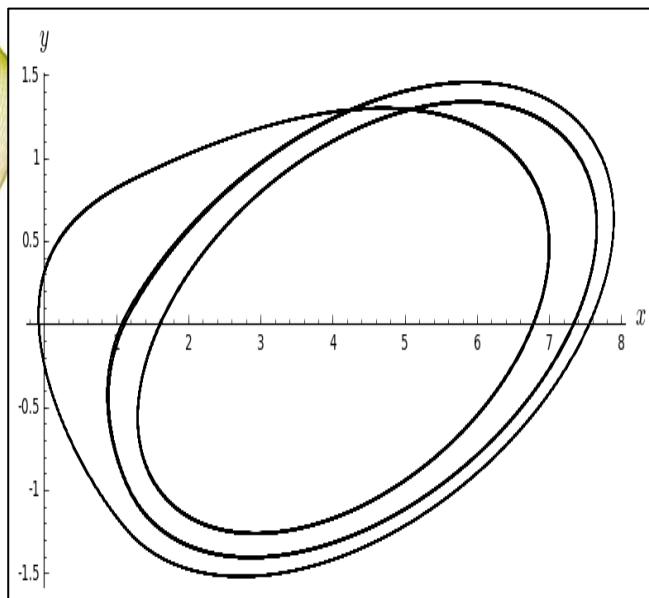
$R = 1998 [\Omega]$



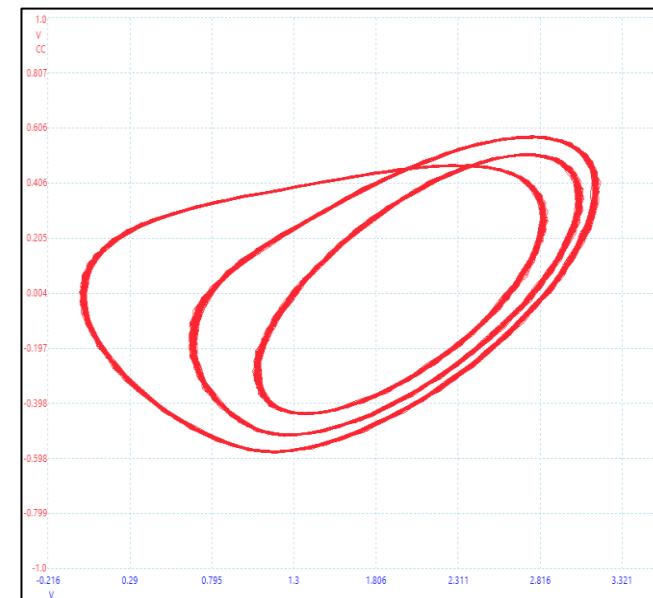
$R = 1701 [\Omega]$

$\Delta = 14.86\%$

# Numerical VS Experimental



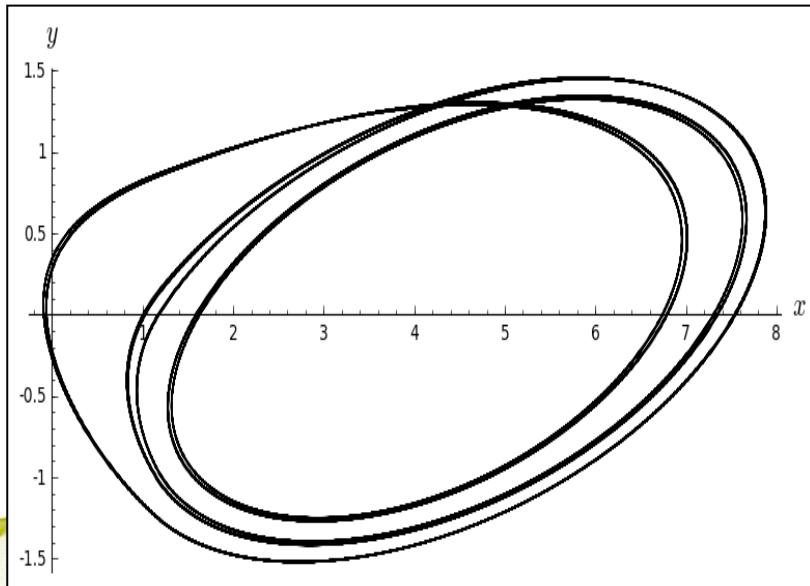
$R = 1993 \text{ } [\Omega]$



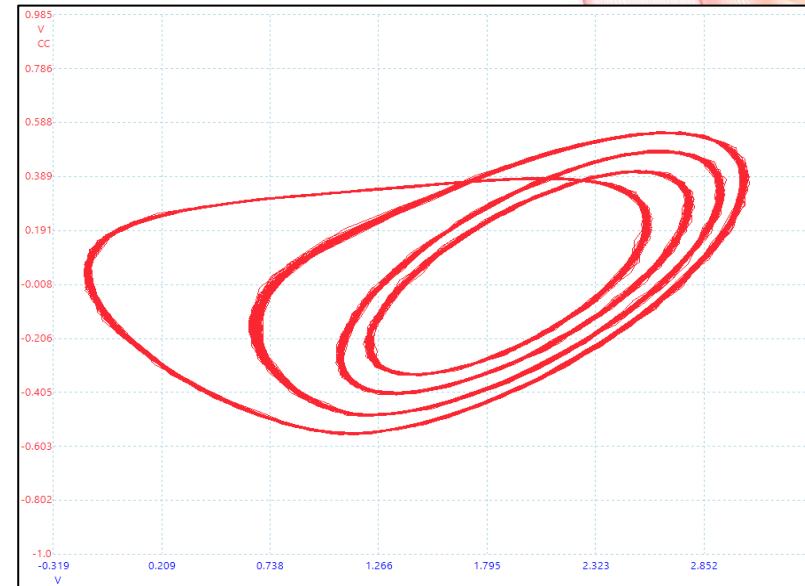
$R = 1677 \text{ } [\Omega]$

$\Delta = 15.85\%$

# Numerical VS Experimental



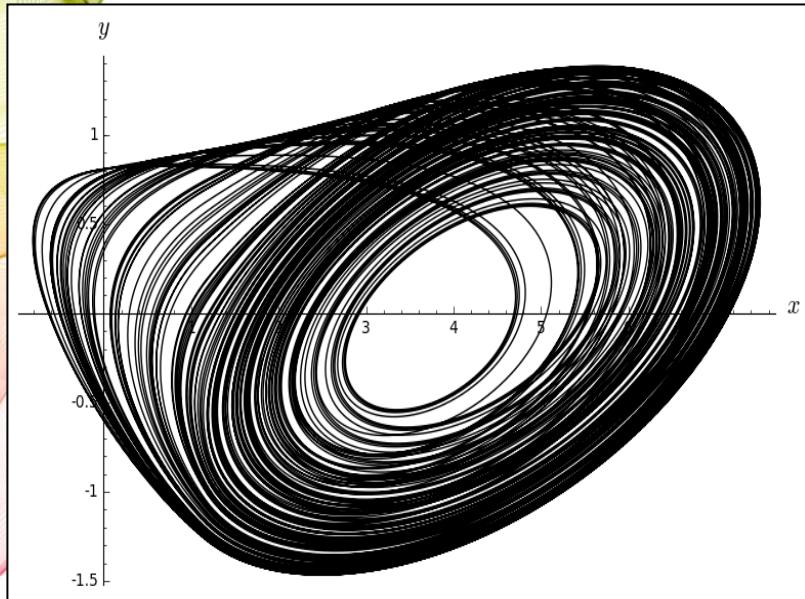
$R = 1992 [\Omega]$



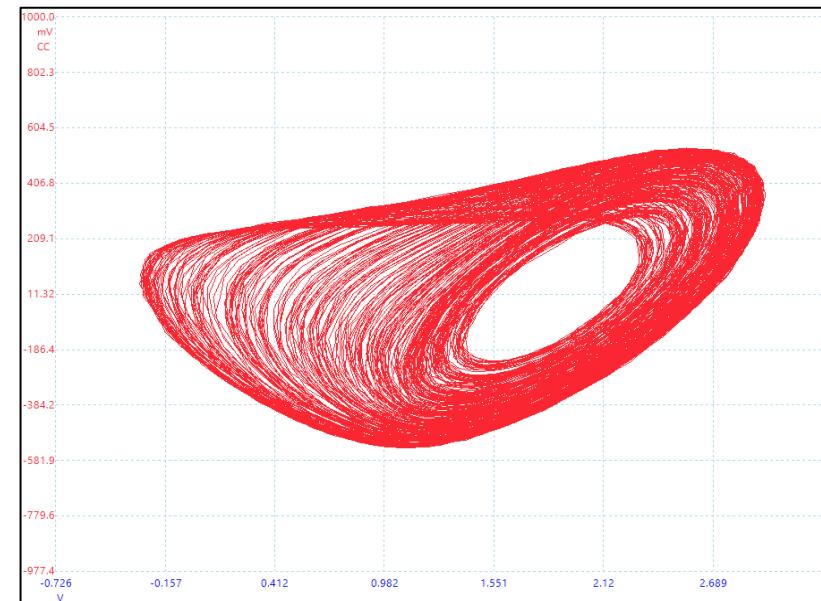
$R = 1669 [\Omega]$

$\Delta = 16.21\%$

# Numerical VS Experimental



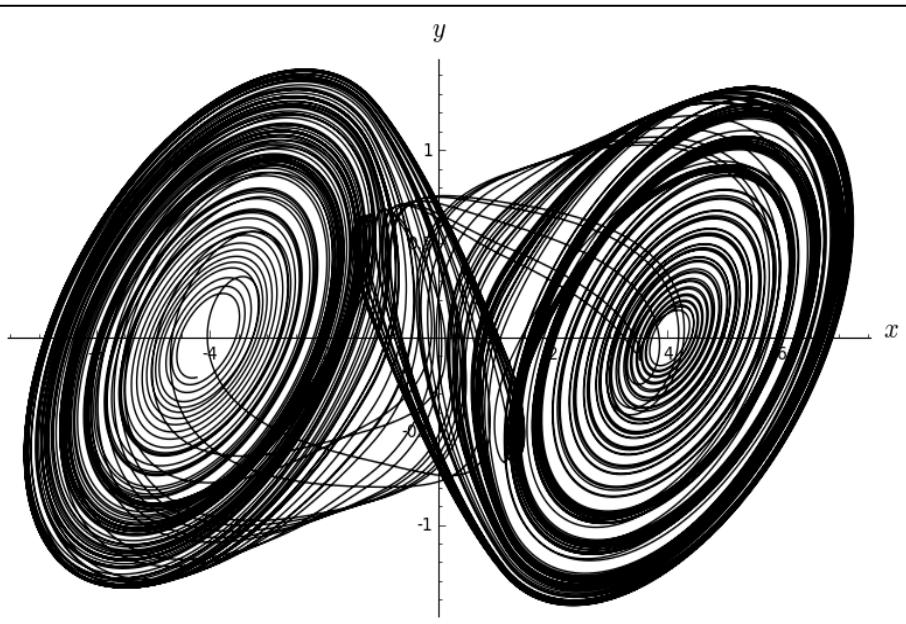
$R = 1974 [\Omega]$



$R = 1650 [\Omega]$

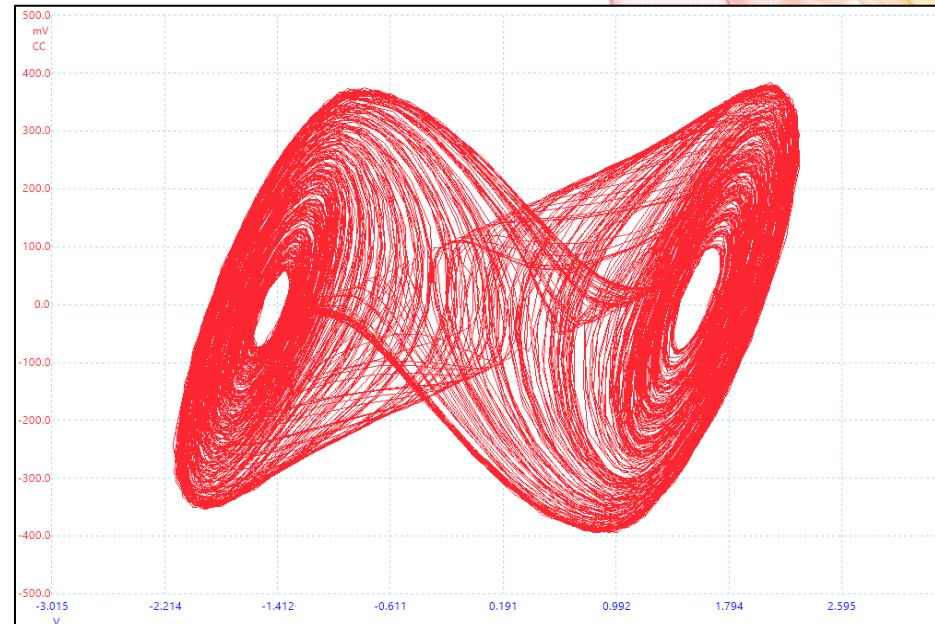
$\Delta = 16.41\%$

# Numerical VS Experimental



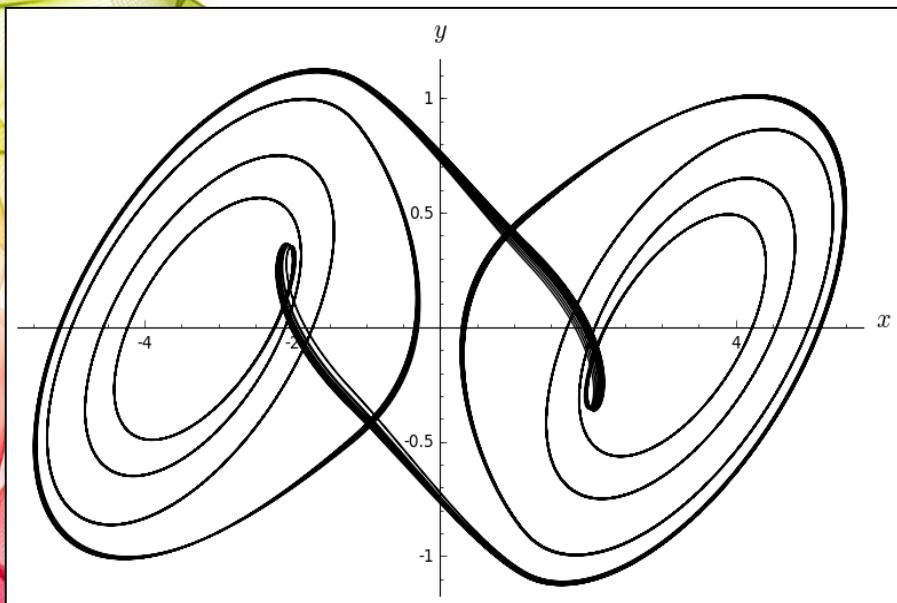
$R = 1961 [\Omega]$

$\Delta = 17.03\%$

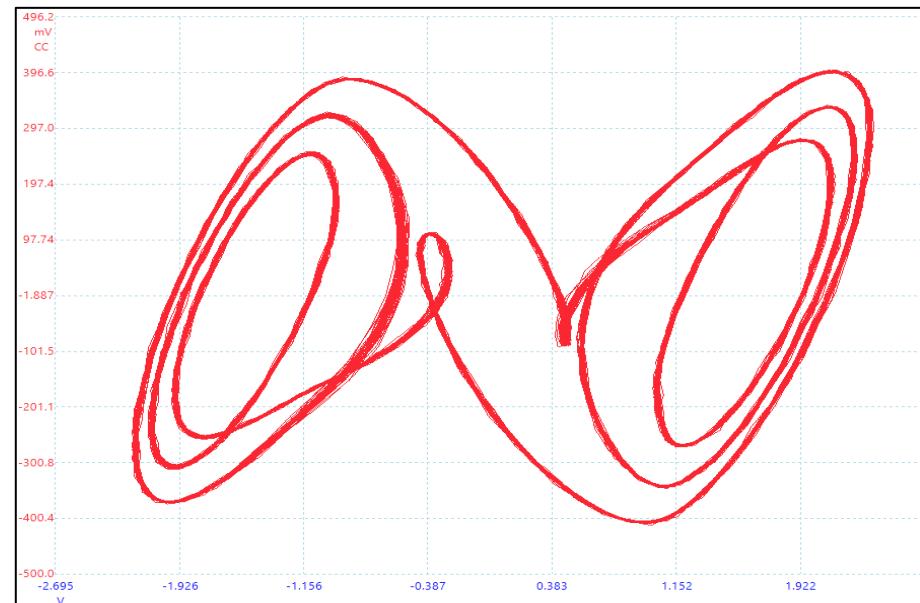


$R = 1627 [\Omega]$

# Numerical VS Experimental



$$R = 1955 \text{ } [\Omega]$$

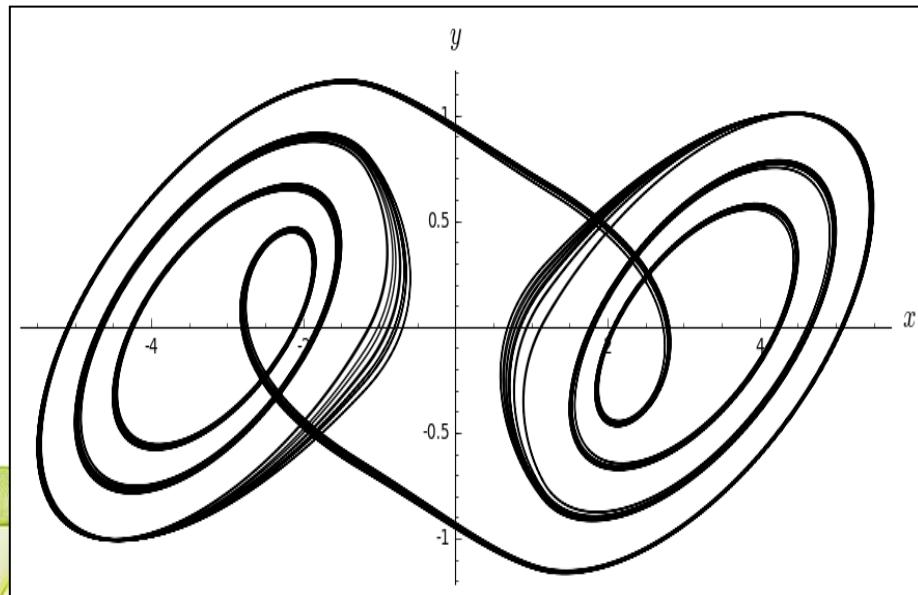


$$R = 1614 \text{ } [\Omega]$$

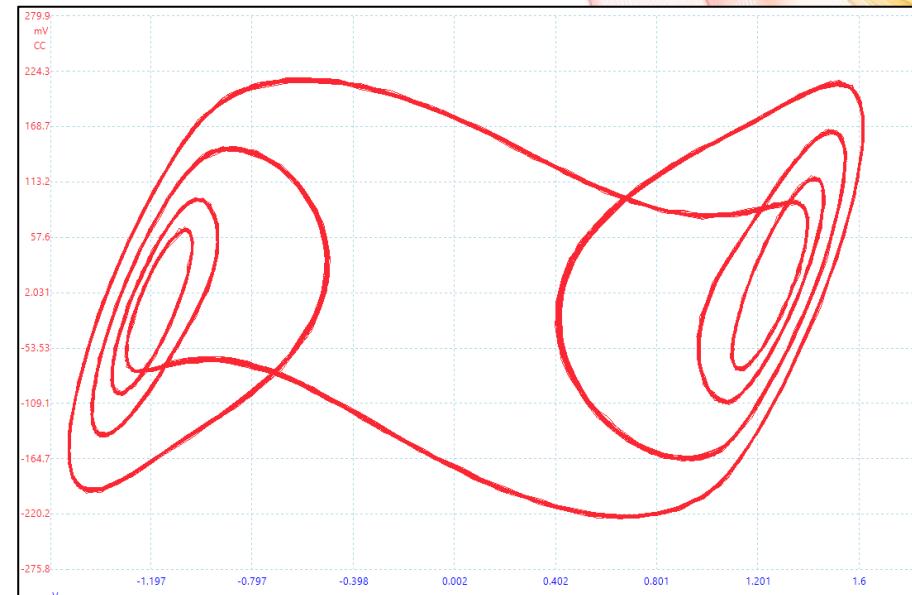
*(Not the same limit cycle ... )*

$$\Delta = 17.44\%$$

# Numerical VS Experimental



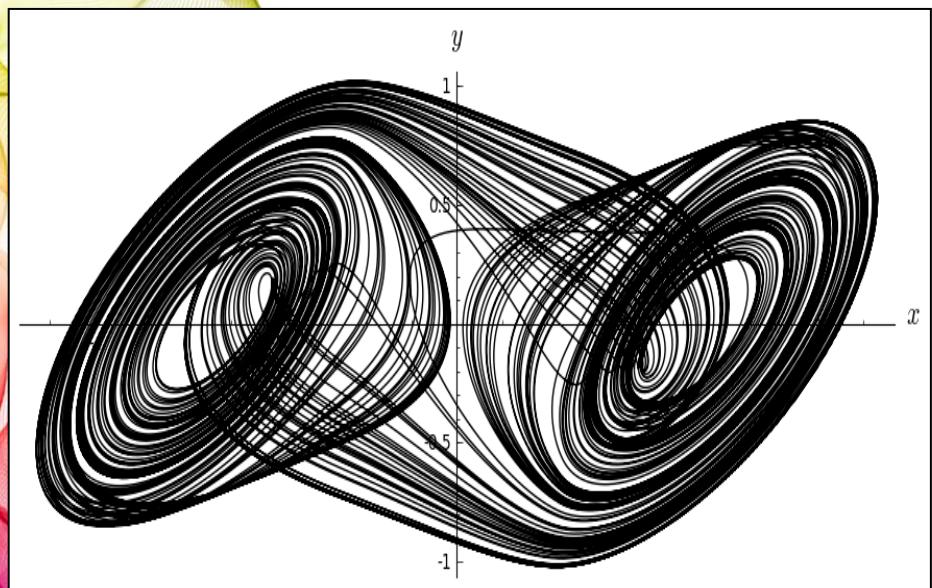
$R = 1851 \text{ } [\Omega]$



$R = 1607 \text{ } [\Omega]$

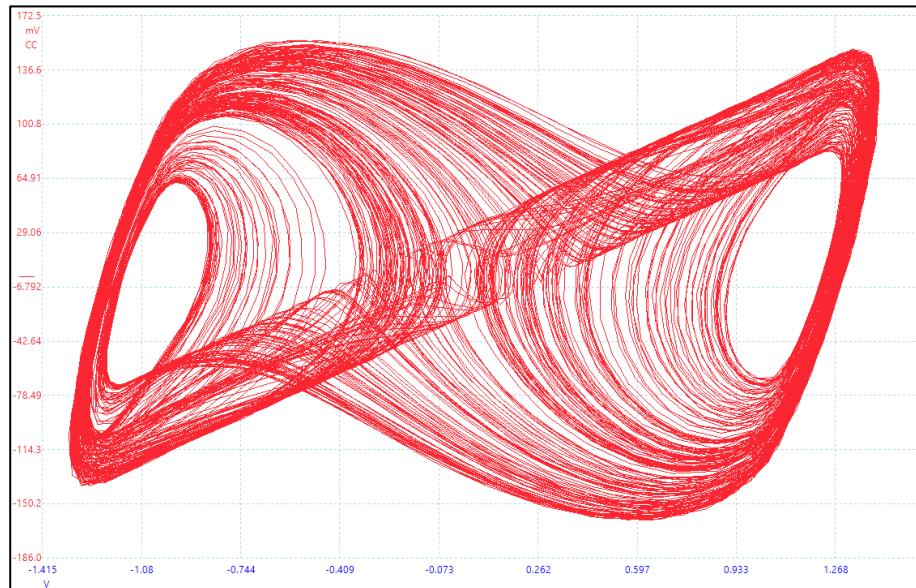
$\Delta = 13.18\%$

# Numerical VS Experimental



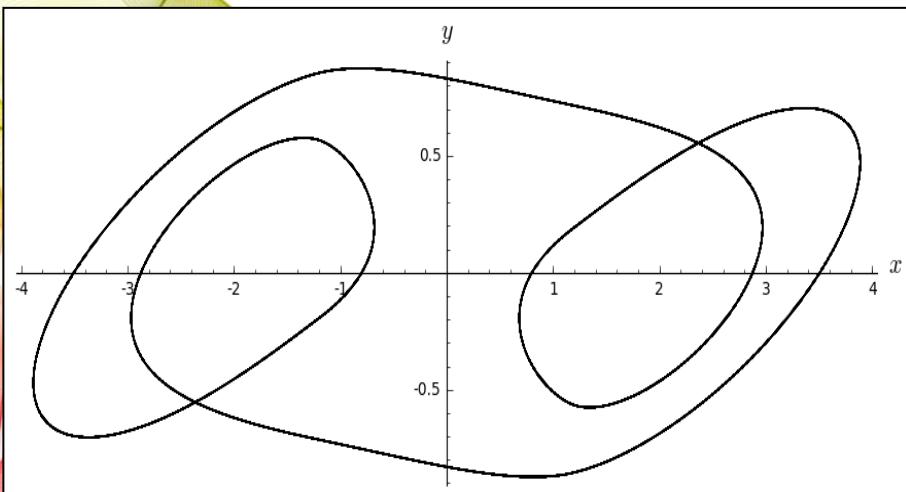
$R = 1783 \text{ } [\Omega]$

$\Delta = 14.07\%$



$R = 1532 \text{ } [\Omega]$

# Numerical VS Experimental



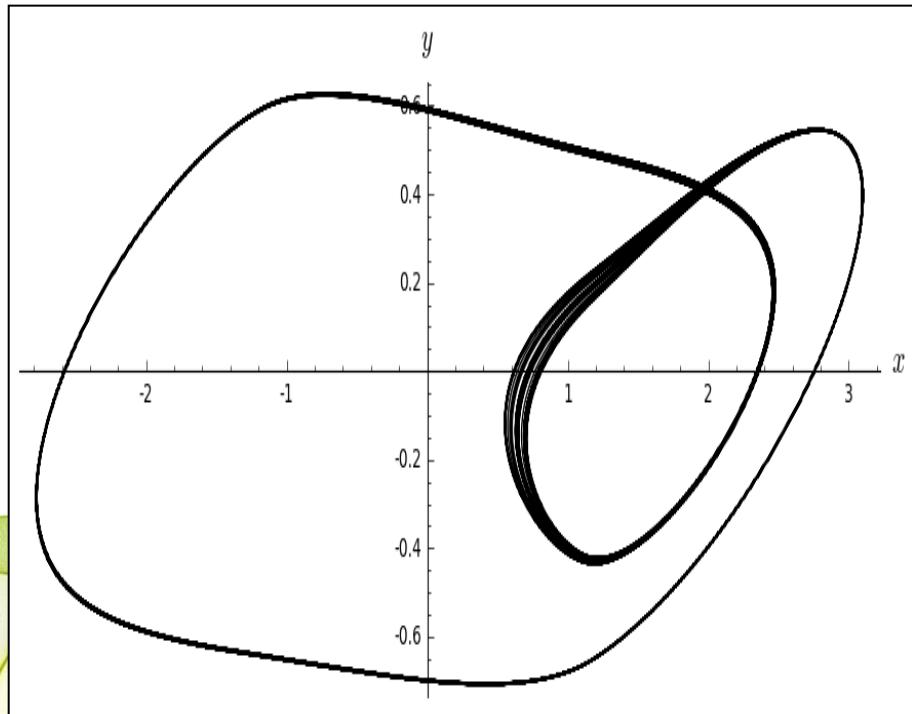
$R = 1706 \text{ } [\Omega]$



$R = 1427 \text{ } [\Omega]$

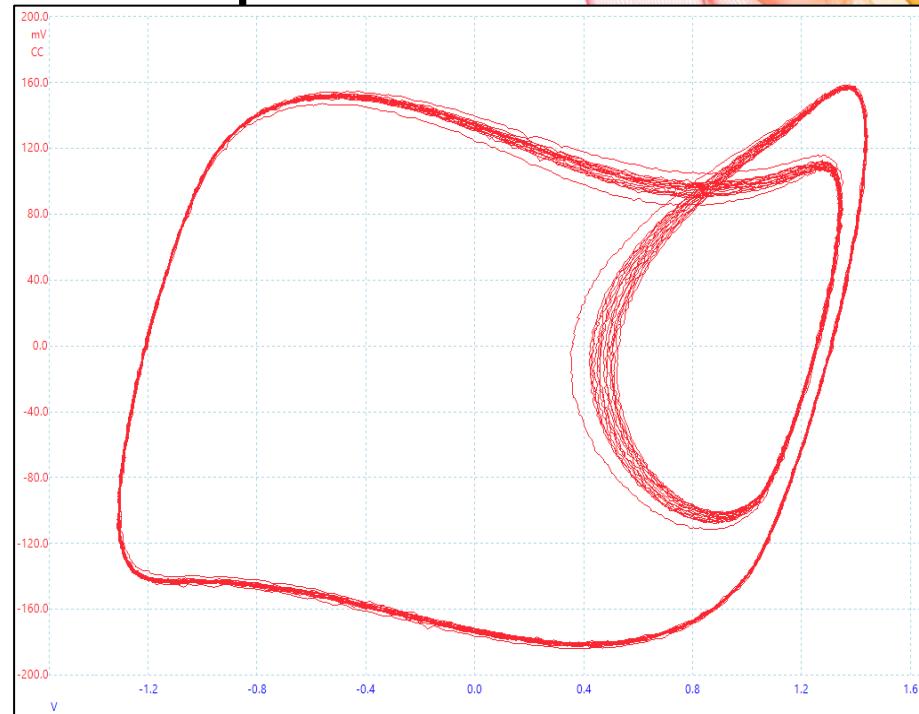
$\Delta = 16.35\%$

# Numerical VS Experimental



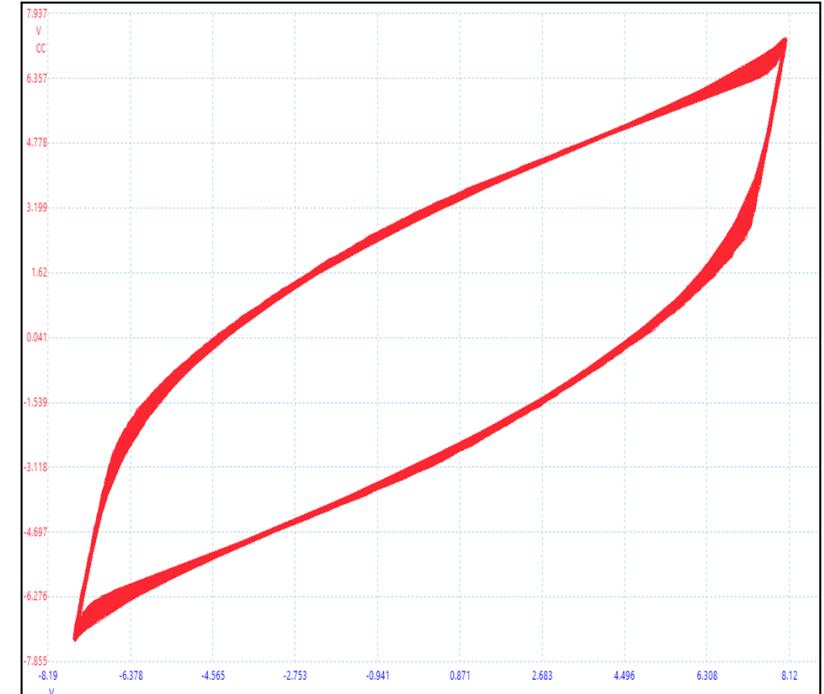
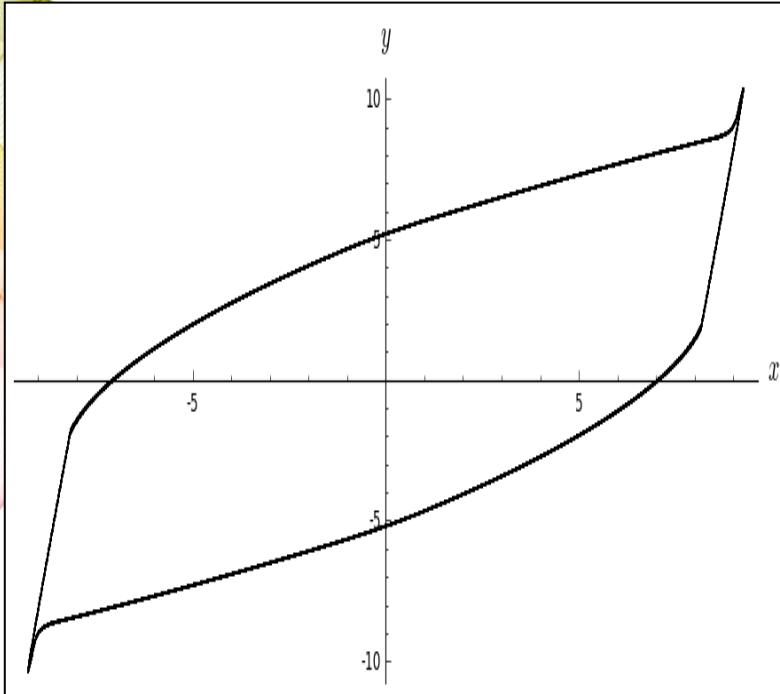
$R = 1610 [\Omega]$

$\Delta = 18.81\%$



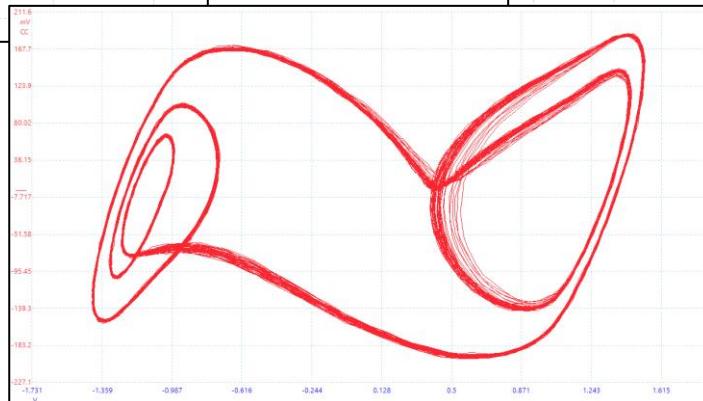
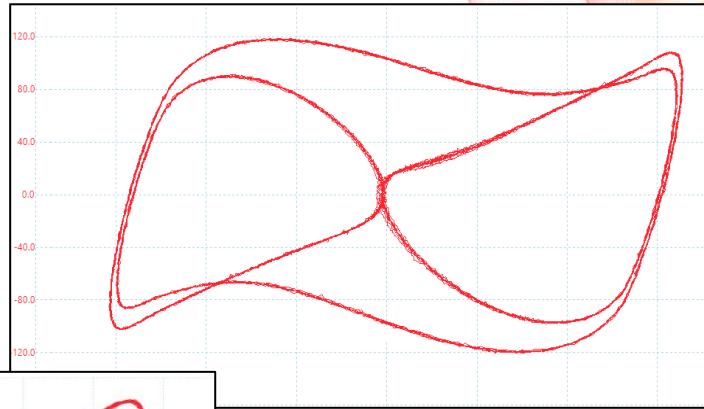
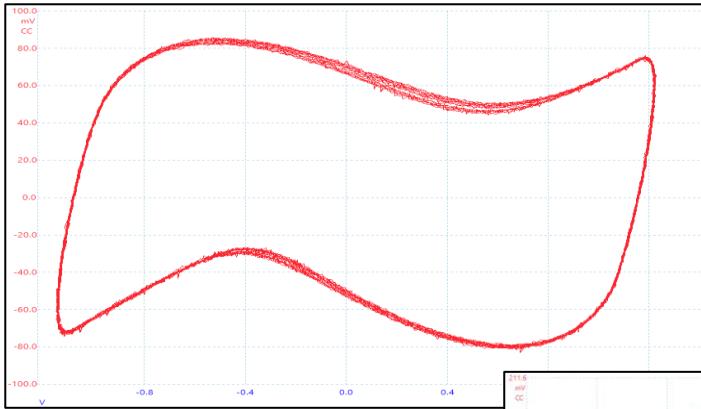
$R = 1307 [\Omega]$

# Numerical VS Experimental



The outmost limit cycle

# Experimental: Dancing around the outmost limit cycle

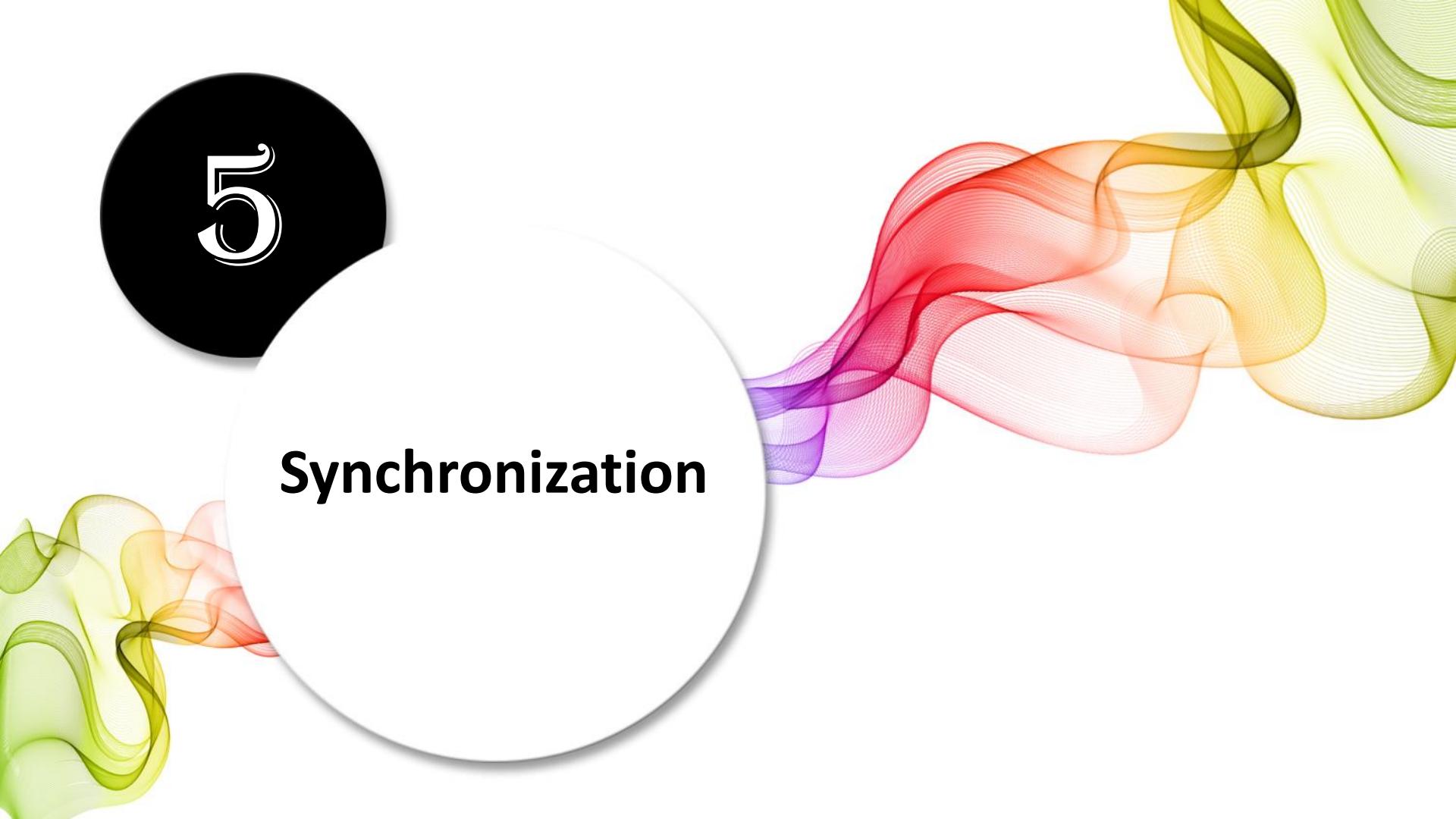




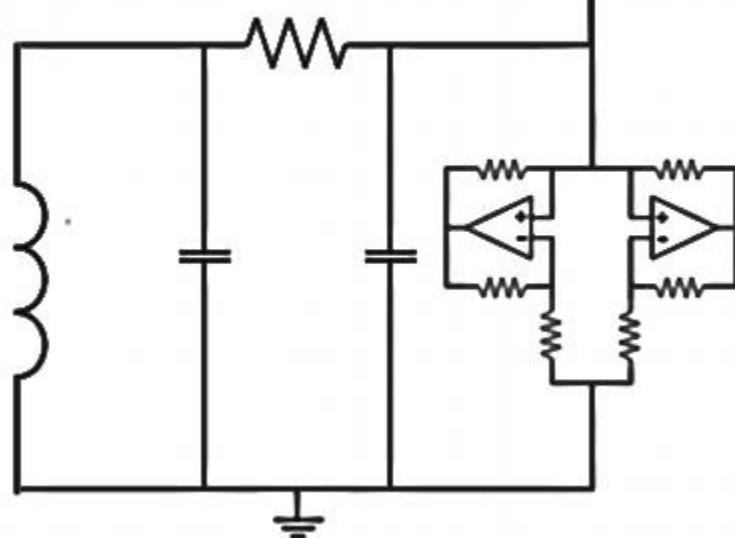
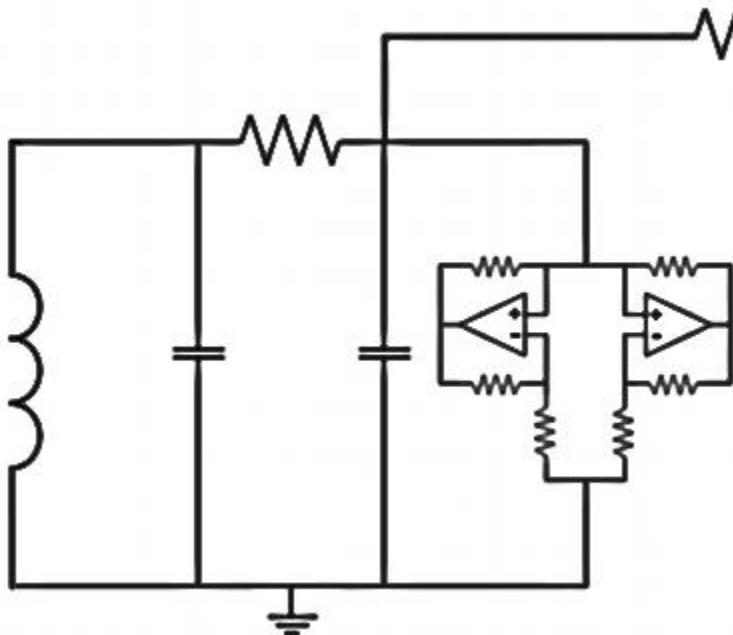
5



# Synchronization

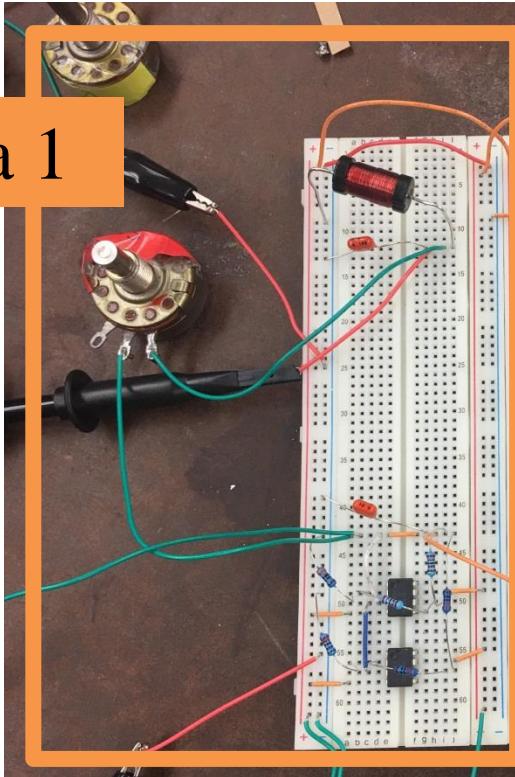


# Bidirectional Chua's Circuit

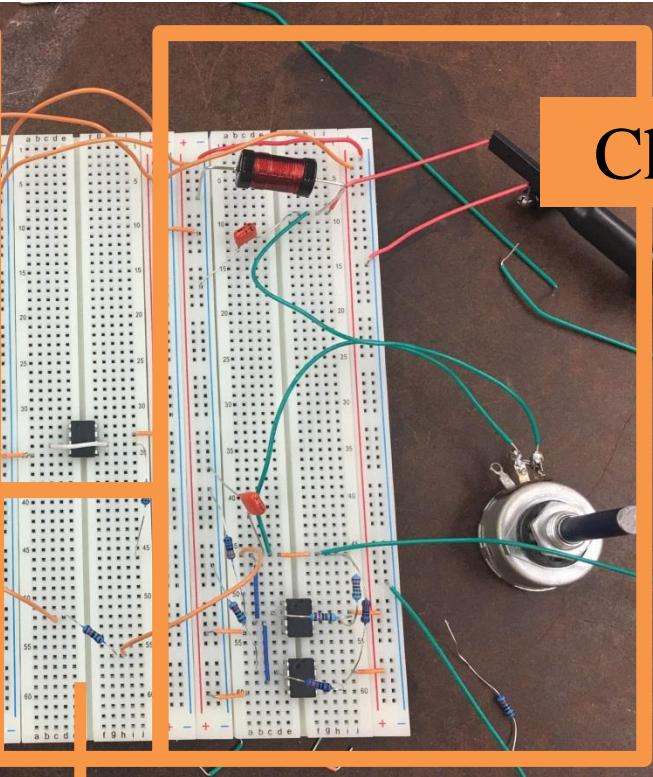


# Experimental Realization

Chua 1

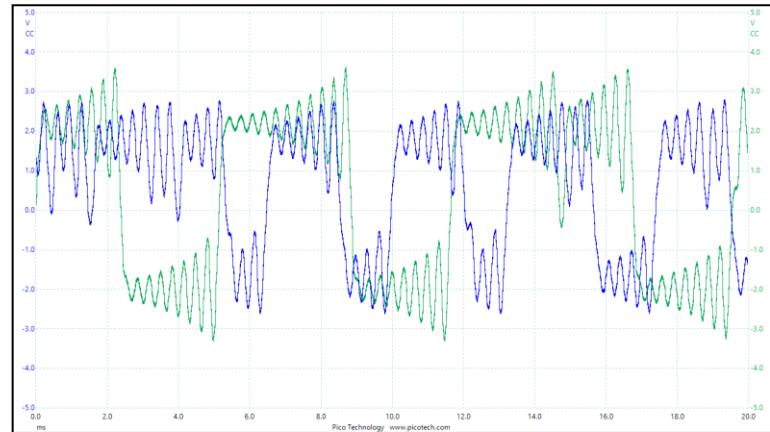
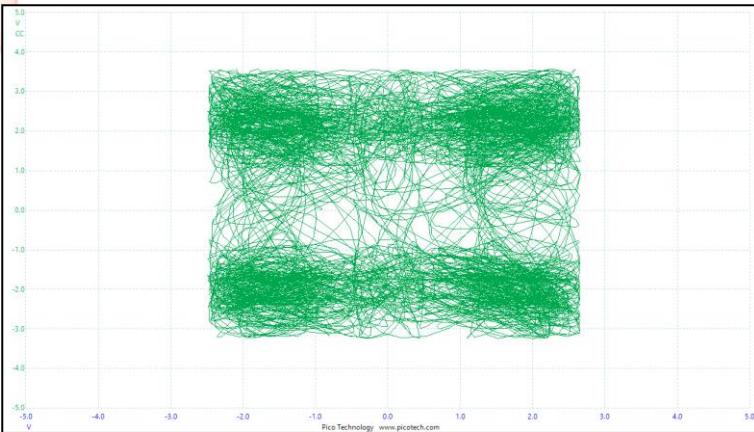
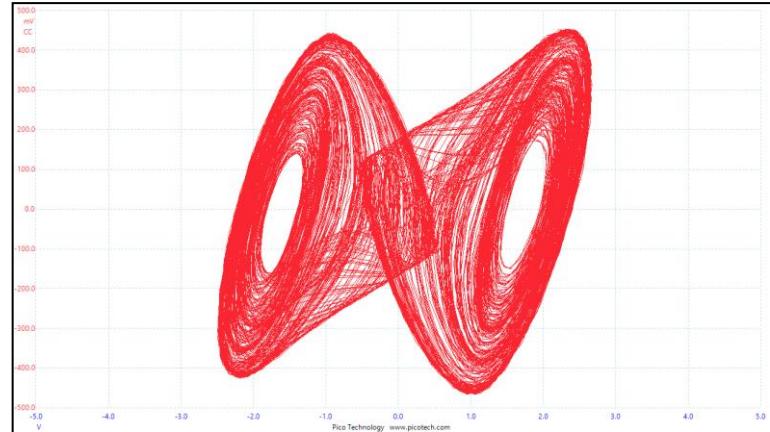
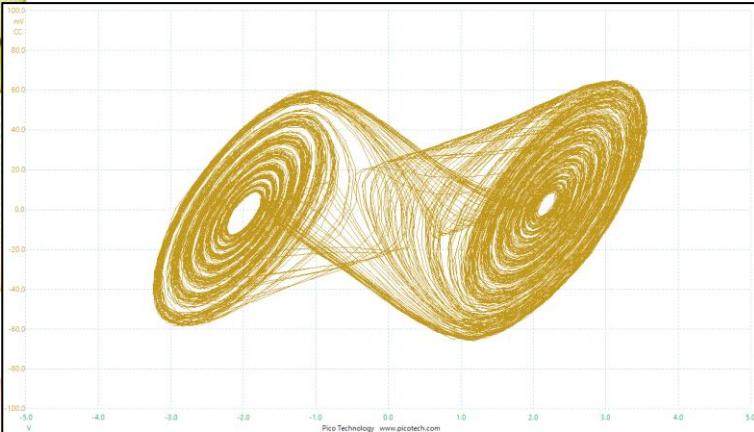


Chua 2

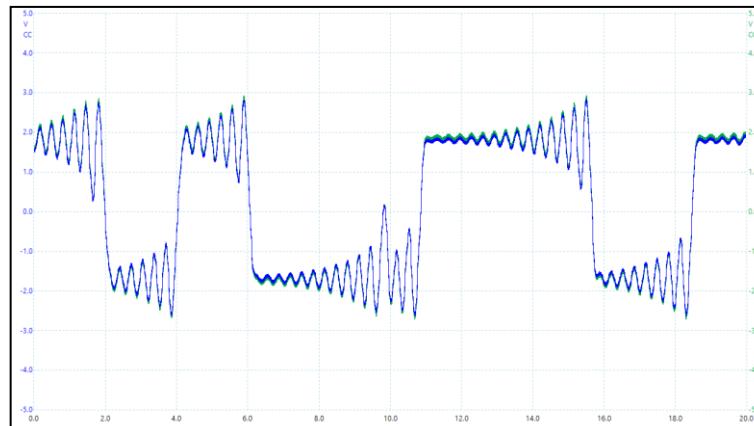
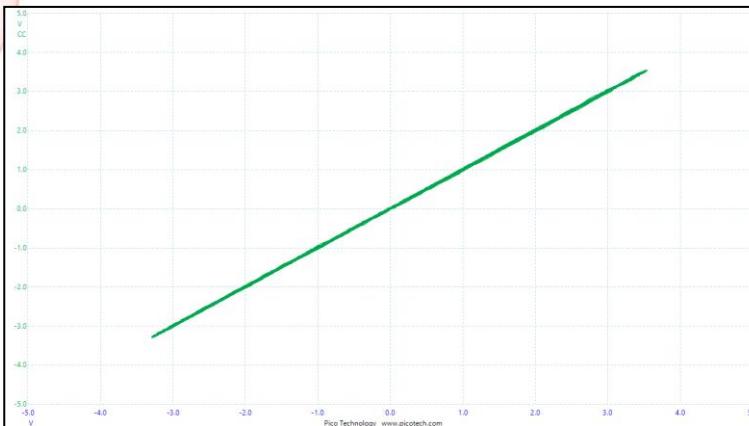
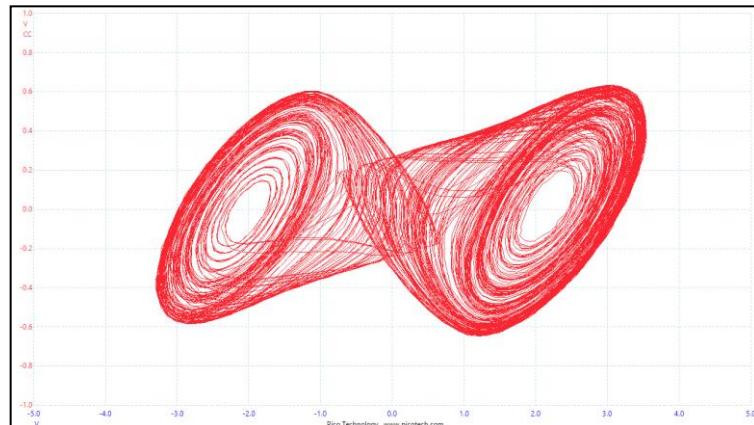
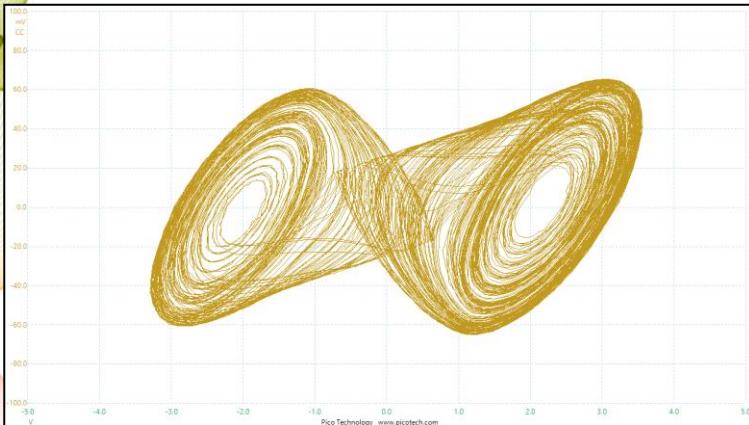


Synchronization Resistor

# Bidirectional Chua's Circuit



# Bidirectional Chua's Circuit



# List of Sources

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