

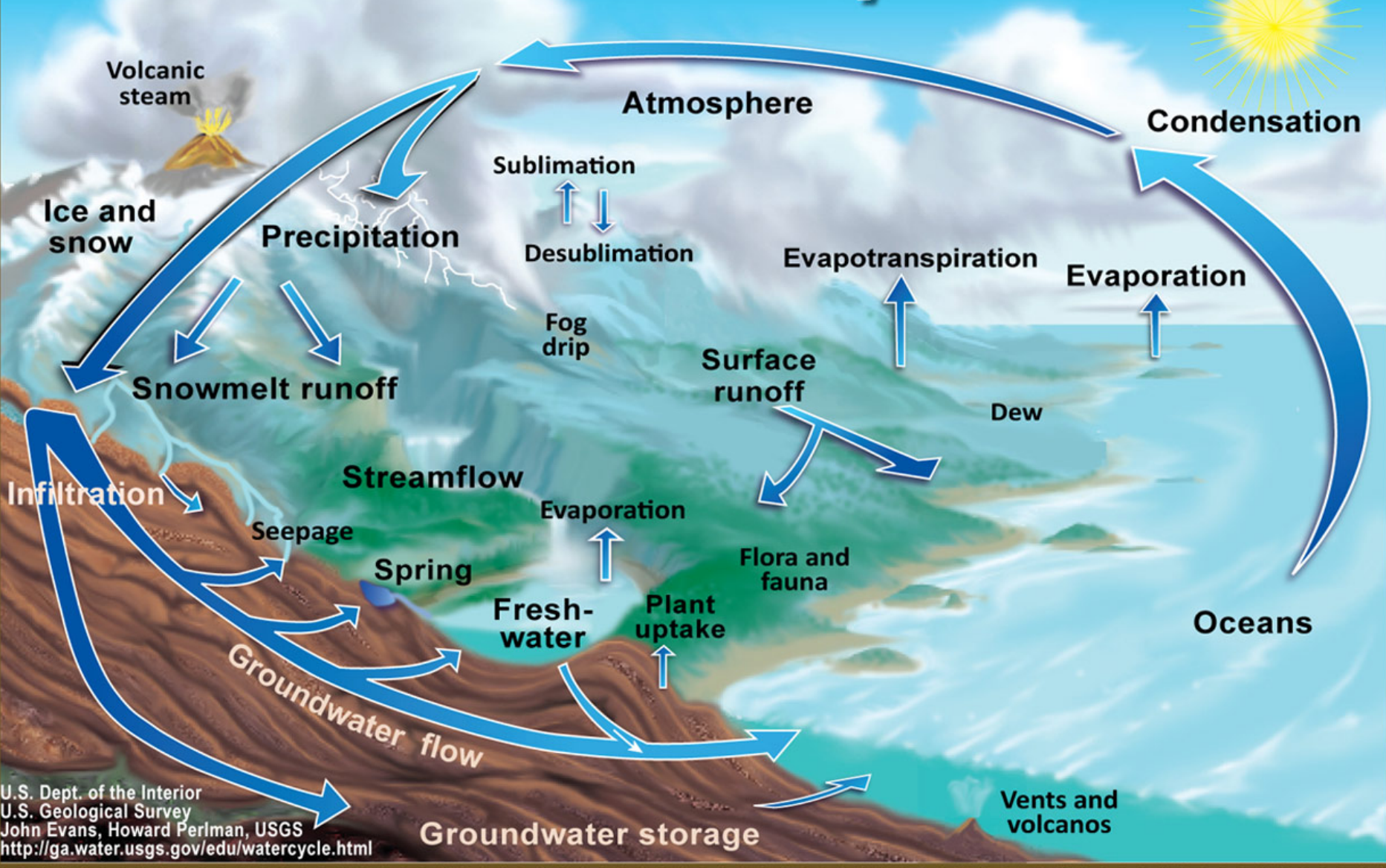
Using Hidden Markov Random Fields for Estimating the Uncertainty in Groundwater Flow

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The Water Cycle



Groundwater Flow

- A form of Diffusion Equation,

$$S \frac{\partial h}{\partial t} = T \nabla^2 h + R$$

Source/Sink
Recharge/Pumping

Aquifer Parameters
Storage & Transmissivity

- *Derived from the continuity equation for a REV where parameters are assumed to be effectively constant - (lab scale),*
- *Darcy's Law is used to describe the fluxes.*

Regional Scale

3 miles

A regional scale map showing groundwater investigation data. The map is color-coded with various shades of yellow, orange, red, and brown, representing different geological or hydrological units. A prominent yellow area is visible in the center. A red horizontal line indicates a scale of 3 miles. The map includes a grid of latitude and longitude lines, with labels such as 'R.13 E', 'T.20 N', and 'T.19 N'. The text '3 miles' is written in red below the scale bar.

Interpolated from point data and field methods!!!
DWR (1967), Northeastern Counties Groundwater Investigation

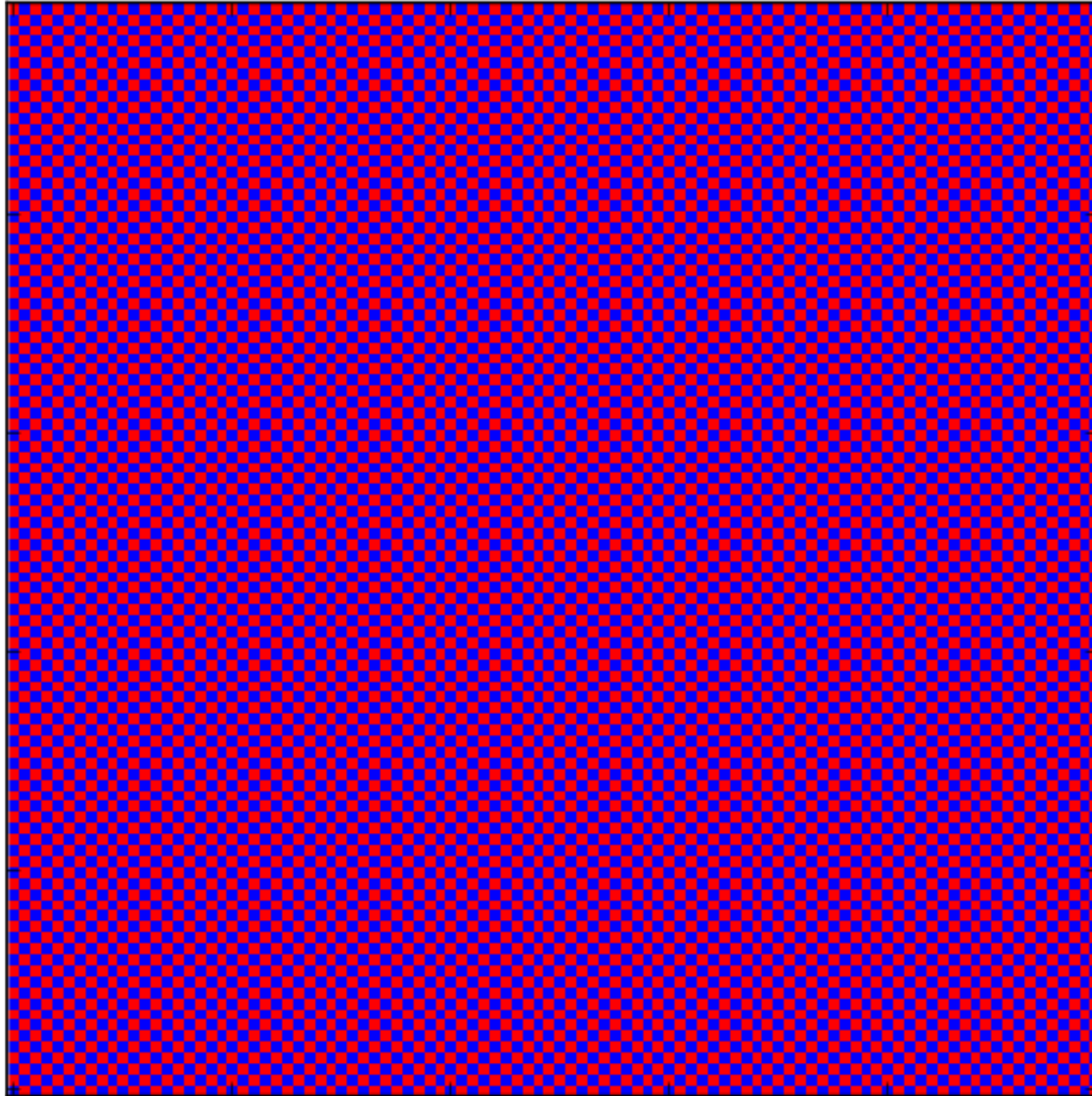
Modeling the Uncertainty

- Monte Carlo simulations, many realizations are needed;
- Often hydrogeologic parameters are assumed to be random constants,
- Rarely Discrete/Continuous Markov Fields are used.

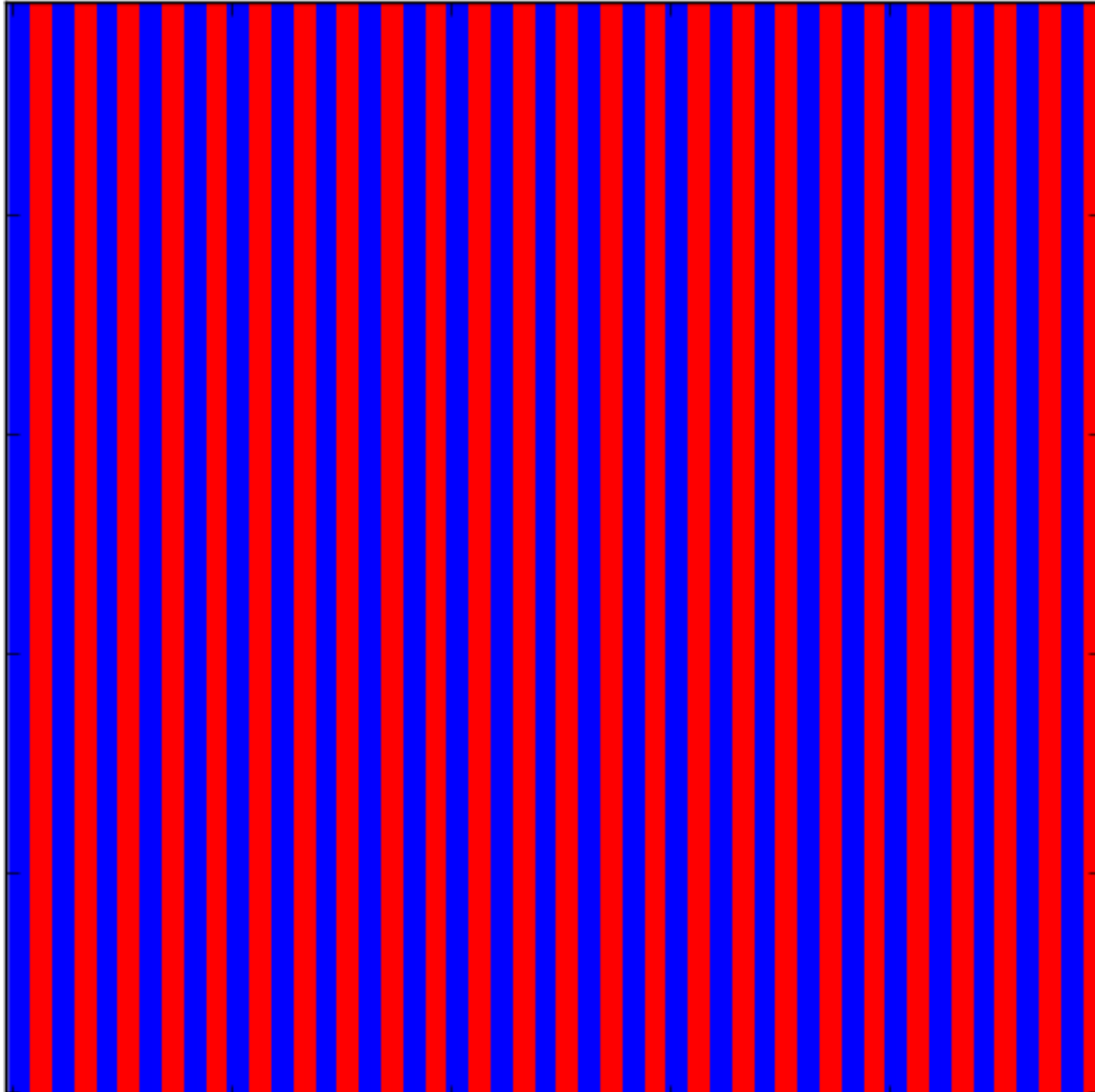
Project Goals

- Estimate the information stored by the system
 - How random the system is?
- Use transition probabilities to generate other possible realizations.

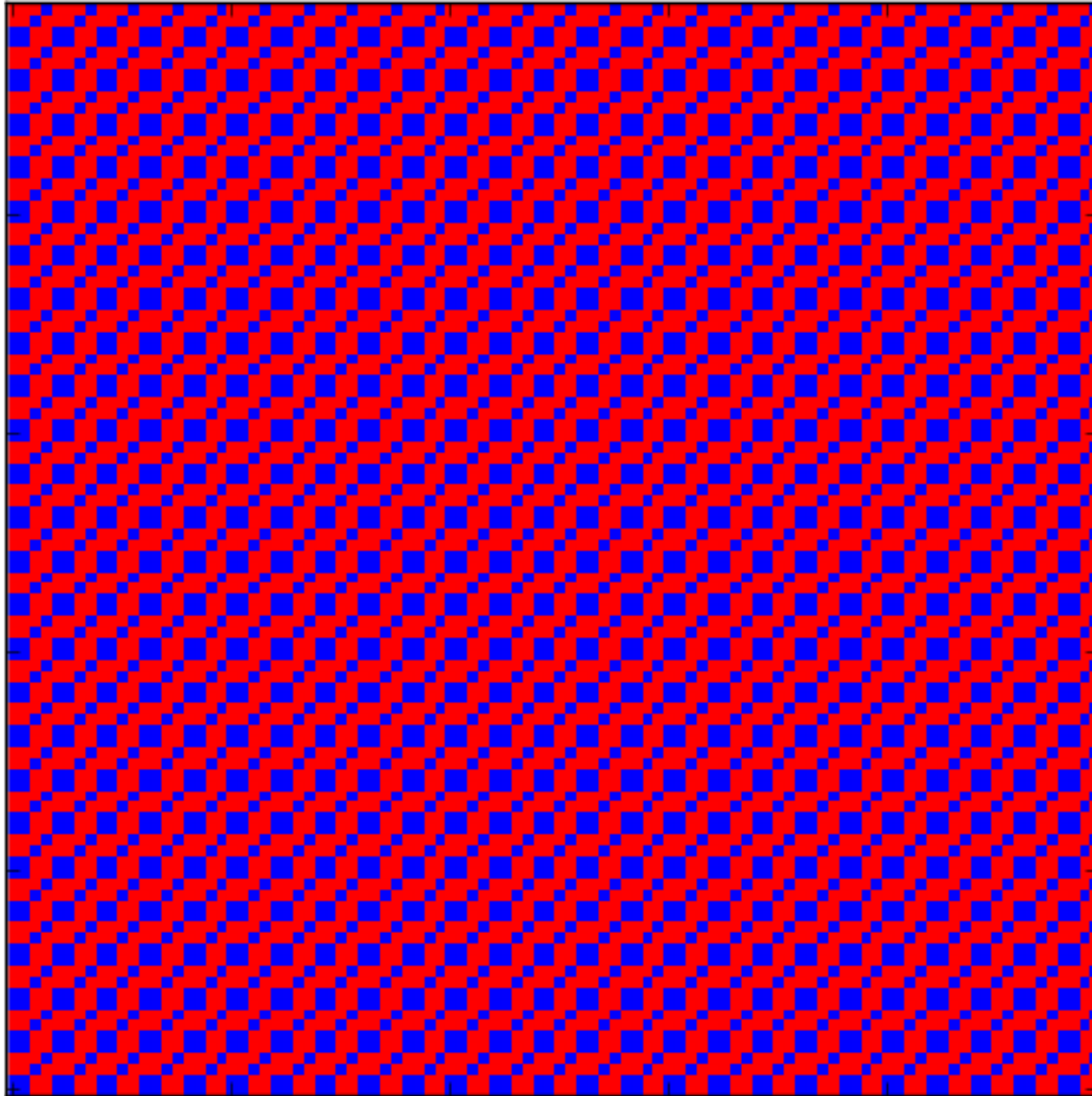
Test Runs



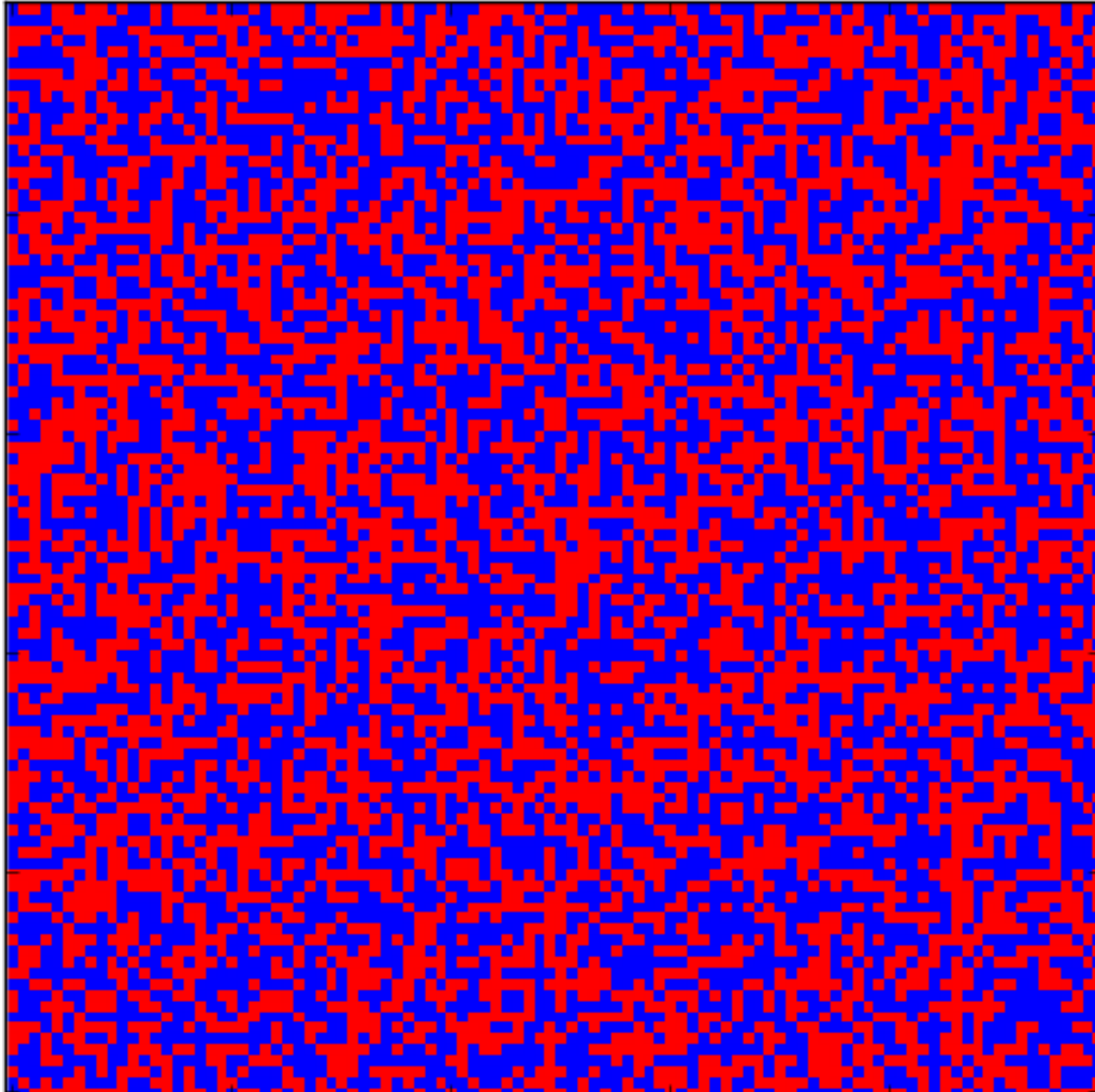
Test Runs



Test Runs



Test Runs



Test Runs

2 unique

$$P = \frac{1}{2}$$

$$H = 1.0$$

■	■	□
□	■	■

11 unique
 $P = \frac{1}{8}, \frac{1}{16}$

$$H = 3.5$$

8 unique

$$P = \frac{1}{8}$$

$$H = 3.0$$

16 unique

$$P = \frac{1}{16}$$

$$H = 4.0$$

Test Runs

2 unique

$$P = \frac{1}{2}$$

$$H = 1.0$$



Blue	Blue	Blue	White	White
White	White	Blue	Blue	Blue

11 unique

$$P = \frac{1}{8}, \frac{1}{16}$$

$$H = 4.4$$

8 unique

$$P = \frac{1}{8}$$

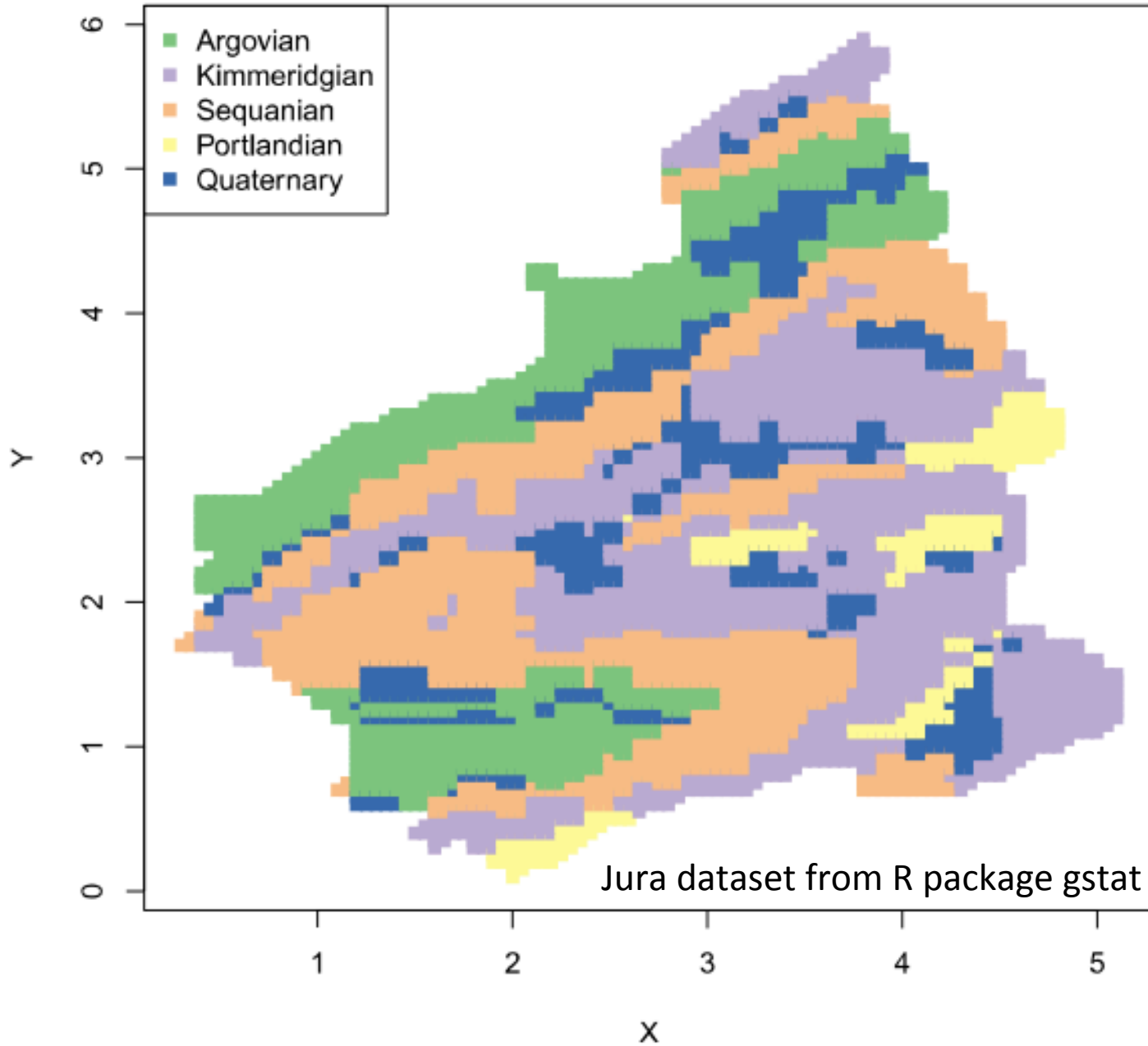
$$H = 3.0$$

16 unique

$$P = \frac{1}{16}$$

$$H = 6.0$$

Swiss Jura geological map



Thanks!